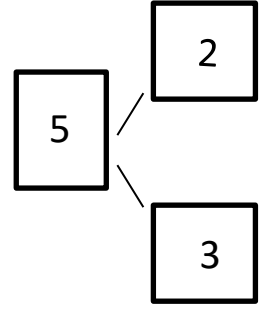
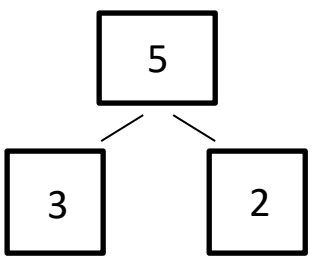




Maths
Calculations Policy
2026

Part, part, whole diagrams are neater if set out in rectangles when children draw them in books rather than cherry diagrams e.g.



This policy has been designed to teach children using concrete, pictorial and abstract methods. This calculation policy should be used to support children to develop a deep understanding of number and calculation alongside the NCETM curriculum prioritisation resources and PD spines.

Background

This policy has been developed by Maths Coordinators with a specific interest in the use of Singapore methods to develop number awareness and fluency.

The policy only details the strategies; teachers must plan opportunities for pupils to apply these; for example, when solving problems, or where opportunities emerge elsewhere in the curriculum.

Using the concrete-pictorial-abstract approach:

Children develop an understanding of a mathematical concept through the three steps (or representation) of concrete-pictorial-abstract approach. Reinforcement is achieved by going back and forth between these representations.

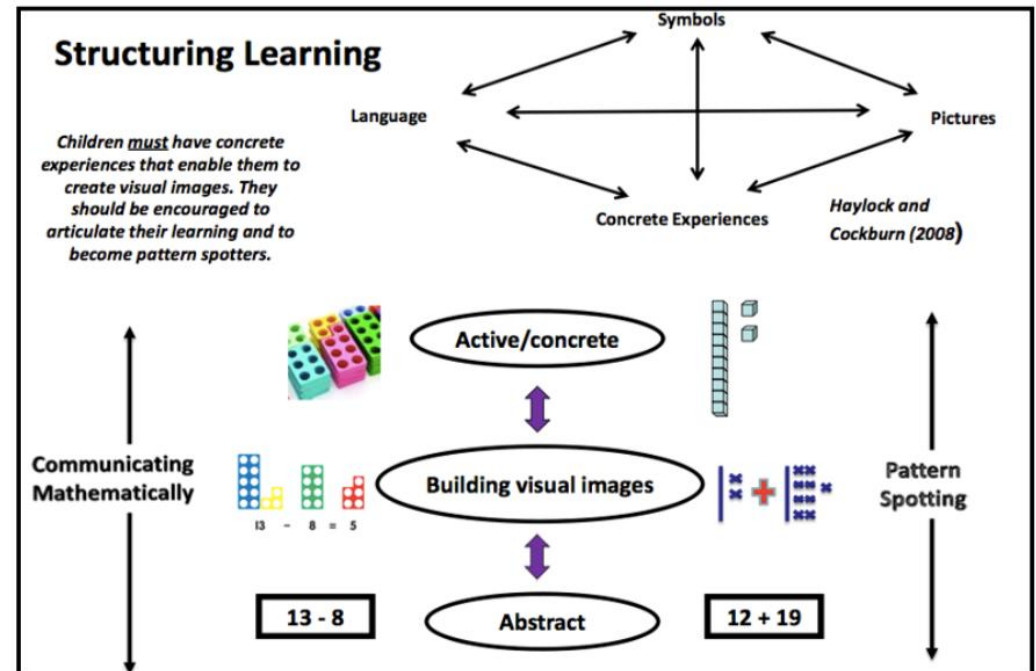
Concrete representation The enactive stage - a pupil is first introduced to an idea or a skill by acting it out with real objects. This is a 'hands on' component using real objects and it is the foundation for conceptual understanding.

Pictorial representation The iconic stage - a pupil has sufficiently understood the hands-on experiences performed and can now relate them to representations, such as a diagram or picture of the problem.

Abstract representation The symbolic stage - a pupil is now capable of representing problems by using mathematical notation, for example: $12 \div 2 = 6$.


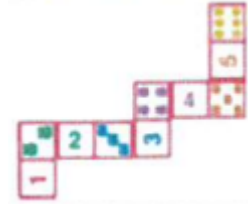
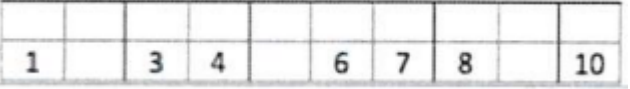
Guidance

This document provides guidance and examples for key objectives for each year group but is not to be followed as a complete planning aid as not all objectives are exemplified.






EYFS Developing Number Sense

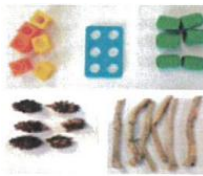

Ordinality:

Concrete	Pictorial	Abstract
<p>Children place a range of physical dominoes in order.</p> 	<p>Children match representations in order.</p> 	<p>Children fill in spaces on a partially filled number track and create representations to show different totals (helping make the link from ordinality to cardinality)</p> 




Ordinal numbers:

Concrete	Pictorial	Abstract
<p>Children line up ducks in a row and verbally label them, e.g. 'first/second/third.'</p> 	<p>Children order pics or slides on IWB of ducks.</p> 	<p>Children apply their understanding of ordinal numbers, e.g. by using written 1st, 2nd and 3rd labels and using verbally language.</p> 

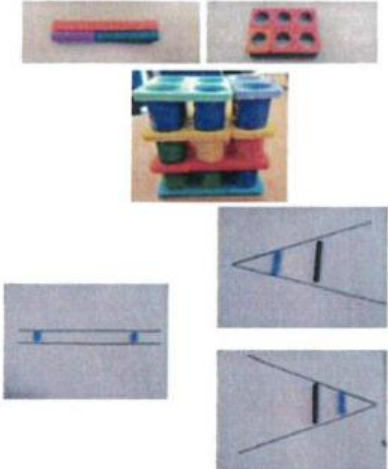
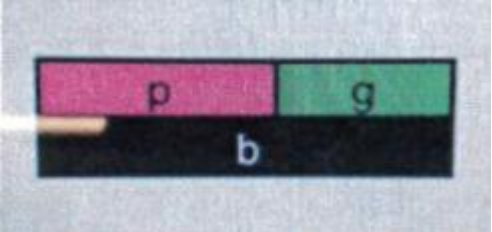
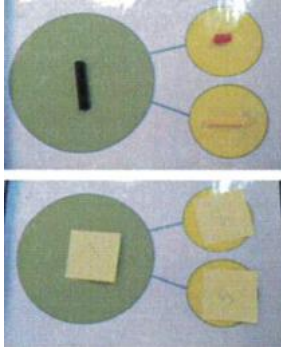
Cardinality:

Concrete	Pictorial	Abstract
<p>Children use a range of structured and unstructured apparatus, inc natural resources, to create different number values.</p> 	<p>Children recognise different number values that are presented in pictorial forms.</p> 	<p>Children are asked a range of questions which show an understanding or cardinality, e.g. Can you find a collection of [objects] to represent six? Can you show me six fingers?</p>







Subitising:

Concrete	Pictorial	Abstract
<p>Children replicate a range of physical representations, which they can then verbally interpret without the need to count objects.</p> 	<p>Children use picture prompts to practice their recognition of number representations and play games on the IWB.</p> 	<p>Children use finger paint to show various 1-6 representations.</p> 







Equality:

Concrete	Pictorial	Abstract
<p>Use physical equipment when learning about equality (and inequality) and use related language, e.g. 'the same as', 'more than and less than.'</p> 	<p>Use pictorial representations to show equality or values that are the 'same as' whilst also verbalizing their reasoning. E.g. 'pink and green are the same as black.'</p> 	<p>Use the cherry model to record either written numerals or pictorial representations that highlight the concept of 'the same as.'</p> 


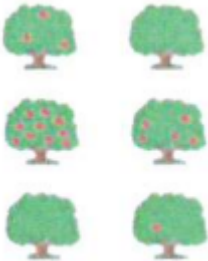

1 to 1 correspondence:

Concrete	Pictorial	Abstract
<p>Count various physical objects by partitioning a group and finally recombining.</p>  <p>Children write a number in each part of a muffin tray and put the appropriate number of buttons in each section.</p> 	<p>Count the dots on the face of a pictorial dice.</p>  <p>Match number cards to pictures of buttons.</p> 	<p>Draw dots to match the number of holes that can be seen on a named Numicon shape.</p>  <p>Cut out buttons equal to the number shown on a number card.</p> 


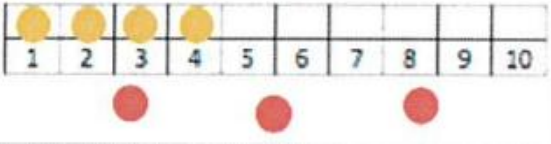


Conservation of number:

Concrete	Pictorial	Abstract
<p>Explore whether the number of cubes stay the same or change when moved around a shape.</p>  <p>Count dolls, put them in rooms then recount to check the total. Agree the total has stayed the same.</p> 	<p>Children work with visual reminders of their concrete experiences – to check their understanding around conservation of number has changed.</p>  	<p>Provide further opportunities to explore and prove their thinking. E.g. put 6 dolls in the house and then move them around. In order to prove there are still 6, they could place them on a number track – applying their understanding of the cardinal principle.</p>  

Concept of zero:

Concrete	Pictorial	Abstract
<p>Use a shuffle box with up to 10 objects in. Children write the corresponding number sentence for where the objects land. E.g. $2=1+1$. Query what happens if there is nothing on one side. Introduce the concept of zero, e.g. $2=2+0$</p> 	<p>Use pictures to see that you can have an amount called 'zero.' Count the apples on the tree and circle the one which has no apples.</p> 	<p>Be encouraged to write written sentences for shuffle box using finger paints, e.g. $5=0+5$.</p>  <p>Grasp the concept of zero to use within number sentences, e.g. $4=4+0$ and verbalise 'I know that four is the same as four add zero.'</p>

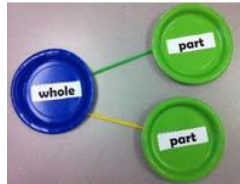
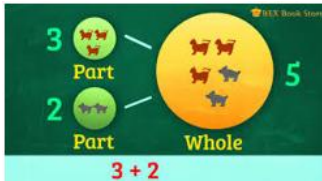
Counting on:

Concrete	Pictorial	Abstract
<p>Use physical objects to learn the skill. E.g. count on from larger value by using their fingers whilst pointing at each 'extra' dot on the second side of the domino.</p> <p>Use counters on number tracks to rehearse counting on.</p>  	<p>Use a die to generate numbers and count on from pictorial representations of counter already positioned on a number track.</p> 	<p>Play games like snakes and ladders.</p> 

EYFS Addition

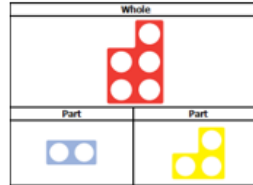
Part, whole, add, more, plus, and, make, altogether, makes, sum, total, how many, greater

Concrete

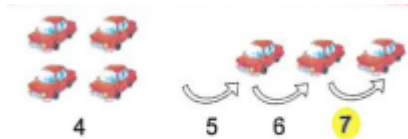


Explore part whole relationships.

Use numicon to develop mental representations of number.



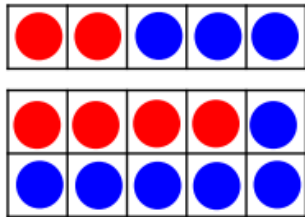
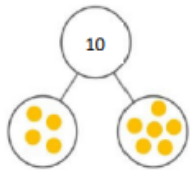
Say which number is one more or one less



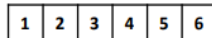
$$4 + 3 = 7$$

Use objects to add 2 single digits by counting on to find answer.

Composing numbers using concrete apparatus such as five / ten frames [working within 10]



Number tracks can be used to support finding one more then a given number.



Addition as increasing by combining two or more groups using concrete apparatus. Children construct calculations verbally or using cards [encourage notations when appropriate]

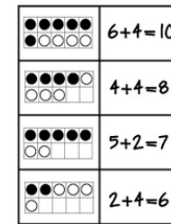


Solving problems – Sara has 2 apples, Jon has 5 apples. How many altogether?

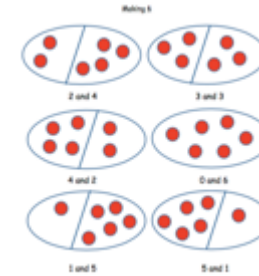


Pictorial

Develop ways of recording calculations using pictures.



Use ten frames drawings to support addition of single digits (counting all/combining two groups)



Count reliably number of objects in a picture and draw the correct amount specified by an adult.



Abstract

Recording one more and one less than calculations

$$4+1=5$$

$$7-1=6$$

Partitioning numbers

$$8 = 8+0$$

$$8 = 7+1$$

$$8 = 6+2$$

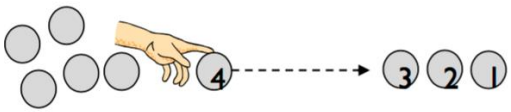
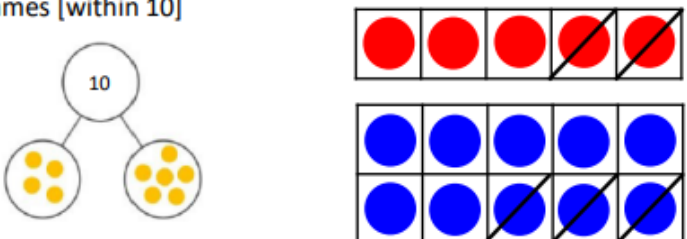
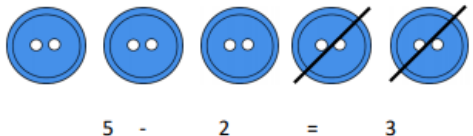

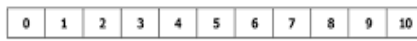
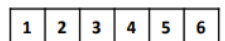
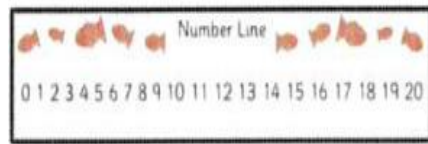
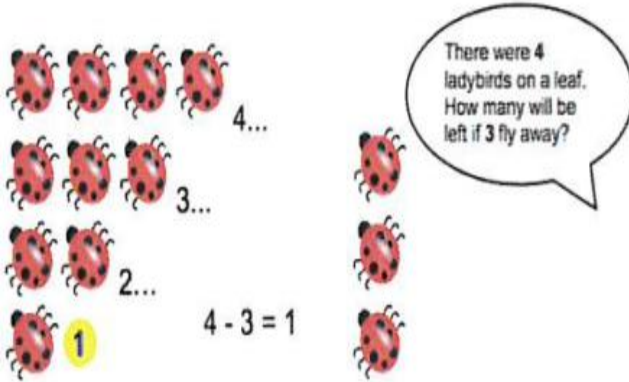
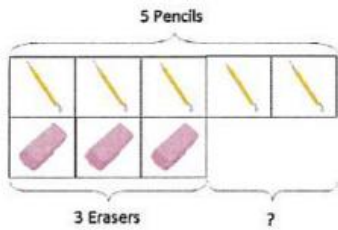
$$8 = 5+3$$

Etc.

Writing calculations to show how a group increases when more are added alongside a verbal story
E.g. There were 5 cars and 4 more cars arrived. There are now 9 cars. $5+4=9$


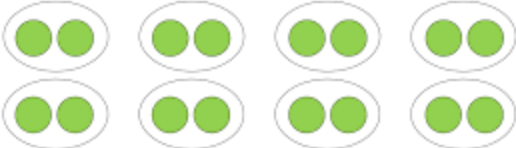
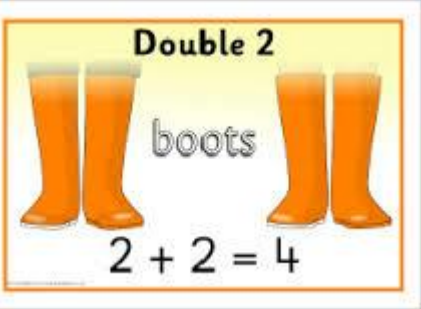



EYFS Subtraction

Part, whole, equal to, take away, less, minus, subtract, leaves, difference between, how many more, how many fewer, less than, most, least, count back, how many left, how much less is ?, left over, how many are gone

Concrete	Pictorial	Abstract
<p>Taking away after counting out practical equipment. . Children would be encouraged to physically remove these using touch counting.</p>  <p>By touch counting and dragging in this way, it allows children to keep track of how many they are removing so they don't have to keep recounting. They will then touch count the amount that are left to find the answer.</p> <p>Those who are ready may record their own calculations</p> <p>Decomposing numbers using concrete apparatus such as five / ten frames [within 10]</p>  <p>Subtraction as decreasing, taking away and finding the difference using concrete apparatus. Children construct calculations verbally or using cards [encourage notations when appropriate]</p>  <p>Use the ten frame to support subtraction by taking away.</p>  $8 - 4 = \underline{\quad}$  <p>Number tracks can be used to support finding one less than a given number.</p> 	<p>The first step to subtraction is being able to count backwards. Use pictures to subtract against a numberline.</p>  <p>Let's count backwards from 14!</p> <p>Use counting back to solve subtractions of pictures.</p>  <p>There were 4 ladybirds on a leaf. How many will be left if 3 fly away?</p> <p>Solve problems using concrete and pictorial images.</p> 	<p>Record number sentences when ready alongside concrete and pictures.</p>

EYFS Multiplication

Part, whole, groups of, lots of, doubles, -times, once, twice, repeated addition

Concrete	Pictorial	Abstract
<p>Children will experience equal groups of objects.</p>  <p>Use doubles</p>	<p>$8 \times 2 =$</p>  <p><i>Draw or make 8 groups of 2 objects, then count or add to see how many altogether.</i></p>	<p>Record equal groups as repeated addition $2+2+2+2=8$</p> <p>Doubles $4+4=8$ $5+5=10$</p>
 <p>Practical problem solving – There are 6 pairs of socks. How many socks are there altogether?</p> 	<p>Multiplication can be introduced through repeated addition and doubling related to real life contexts.</p> <p>Can you double the amount of spots on the ladybird?</p>  <p>This can be extended to writing the calculation by using addition [$5+5=10$].</p> <p><u>Exceeding expectation</u> - Children solve practical problems that involve combining groups of 2, 5, or 10.</p> <p>How many wheels are there altogether?</p> 	

EYFS Division

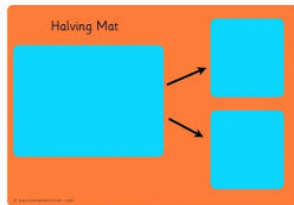
Part, whole, share, share equally, one each, two each, group, groups of, lots of, sharing into groups of, half, one each two each three each etc,

Concrete

Put objects into groups of...

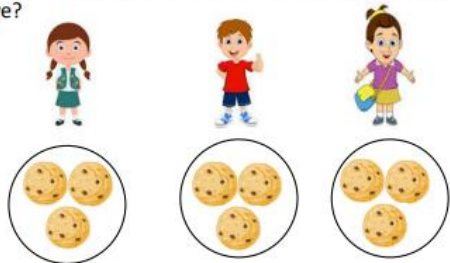


Half as the opposite of doubles



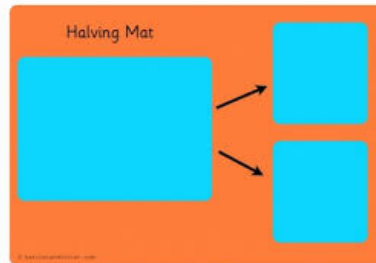
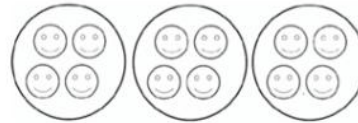
Dividing by sharing into equal groups related to real life contexts.

There are 3 children and 12 biscuits. How many will each child have?



Pictorial

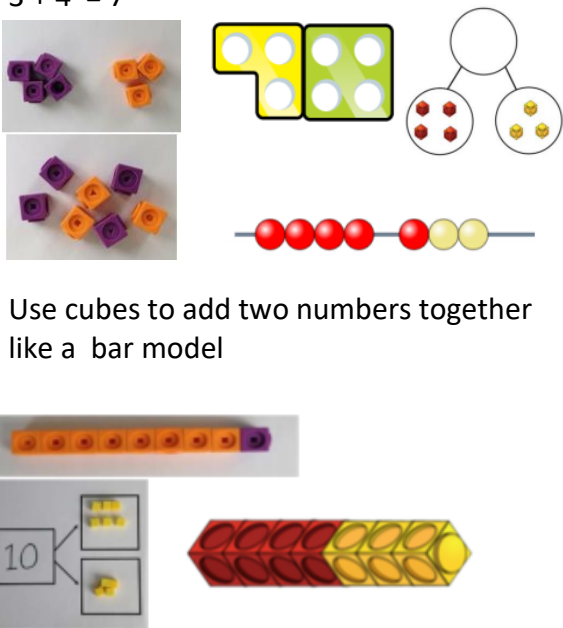
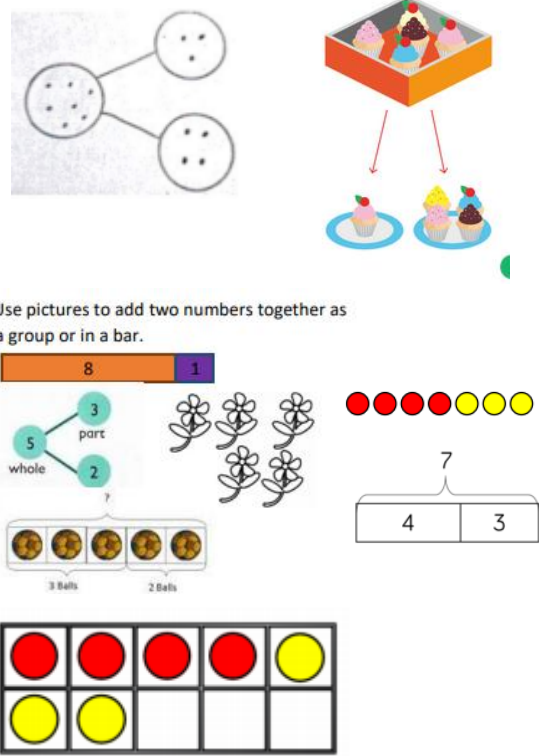
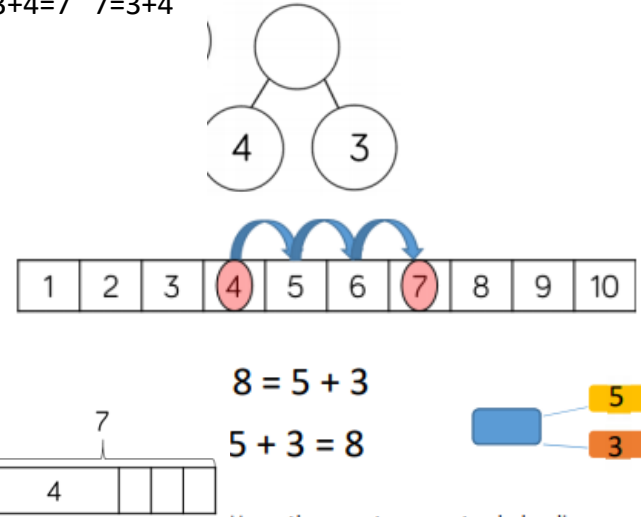
Children will understand equal groups and draw pictures sharing objects out.




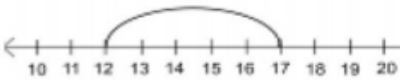
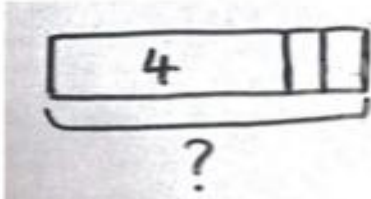
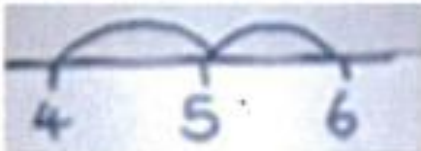



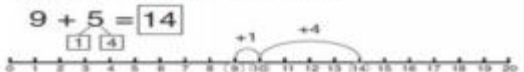



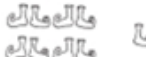
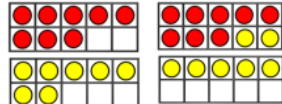
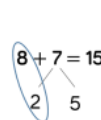
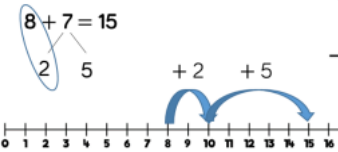
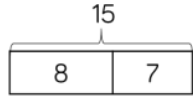



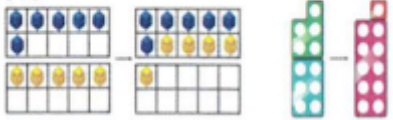
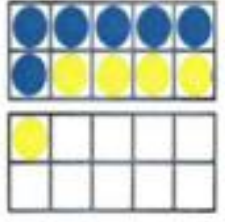
Abstract

Year 1 Addition

Part, whole, addition, add, forward, put together, more than, total, sum, altogether, distance between, difference between, equals, =, same as, most, more, pattern, odd, even, digit, counting on.

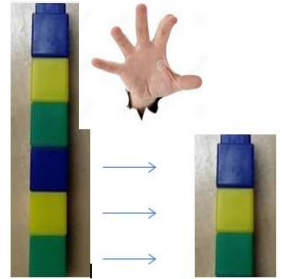
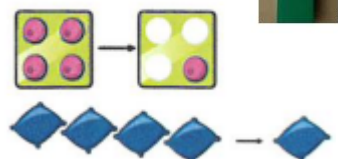
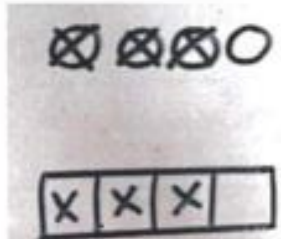
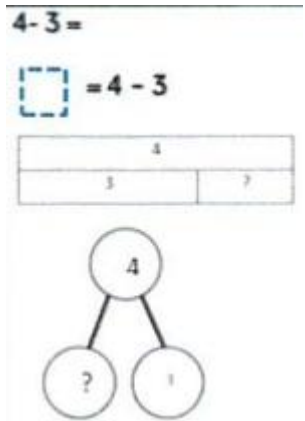
	Concrete	Pictorial	Abstract
<p>Joining two groups and then recounting all objects using one-to-one Correspondence (lots of practice making 10 and numbers to 10 e.g. $6 + 4 = 10$ or $3 + 5 = 8$)</p>	<p style="text-align: center;">$3 + 4 = 7$</p>  <p style="text-align: center;">Use cubes to add two numbers together like a bar model</p>	<p style="text-align: center;">Pictorial</p>  <p style="text-align: center;">Use pictures to add two numbers together as a group or in a bar.</p>	<p style="text-align: center;">Abstract</p> <p>$3+4=7$ $7=3+4$</p>  <p style="text-align: center;">$8 = 5 + 3$ $5 + 3 = 8$</p> <p style="text-align: center;">Use the part part whole diagram as shown above to move into the abstract.</p> <p style="text-align: center;">Include missing number questions to support varied fluency:</p> <p style="text-align: center;">$8 = ? + 3$ $5 + ? = 8$</p>

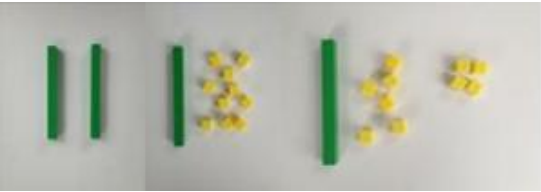
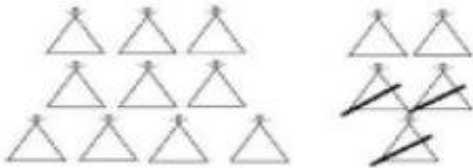
	Concrete	Pictorial	Abstract
<p>Starting at the bigger number and counting on</p>	 <p>Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.</p>  	 <p>$12 + 5 = 17$</p> <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p> <p>A bar model which encourages the children to count on, rather than count all.</p> 	<p>$5 + 12 = 17$</p> <p>Place the larger number in your head and count on the smaller number to find your answer.</p> <p>The abstract number line: What is 2 more than 4? What is the sum of 2 and 4? What is the total of 4 and 2? $4 + 2$</p> 
<p>Regrouping to make 10 (essential later for column addition)</p>	 <p>$6 + 5 = 11$</p>  <p>Start with the bigger number and use the smaller number to make 10. Use ten frames.</p>	 <p>$3 + 9 =$</p> <p>Use pictures or a number line. Regroup or partition the smaller number using the part, part whole model to make 10.</p>  <p>$9 + 5 = 14$</p>	<p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10? How many more do I add on now?</p>
<p>Add and subtract one digit numbers and two digit numbers to 20, including zero</p>	<p>$8 + 1 = 9$</p>  <p>$8 + 7 = 15$</p>  	<p>$8 + 1 = 9$</p>  <p>$8 + 1 = 9$</p> <p>$8 + 7 = 15$</p>   <p>$8 + 7 = 15$</p>	<p>$8 + 1 = 9$</p>  <p>$8 + 7 = 15$</p> 

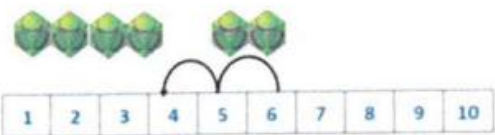
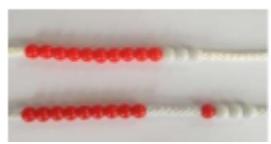
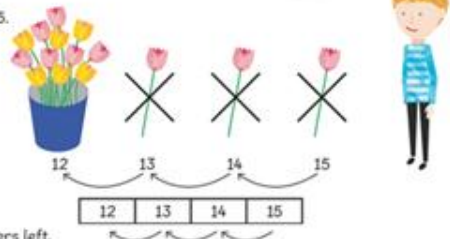
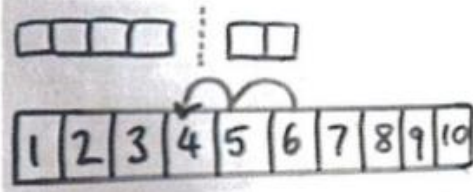
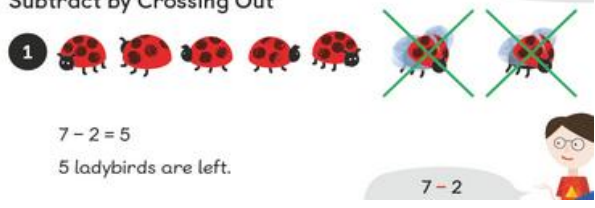
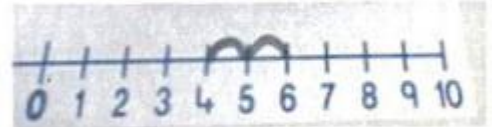
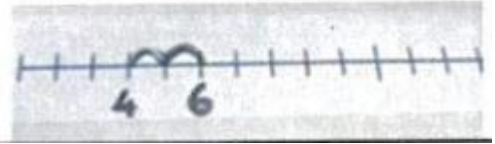
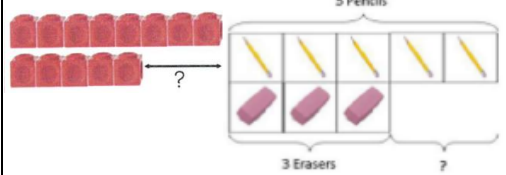
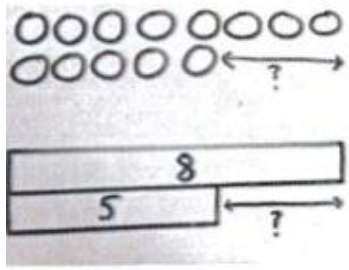
Concrete		Pictorial	Abstract
<p>Bridging 10 Use ten frames, Singapore bars, egg boxes and number lines to practice. <i>Chn should start with the larger number and add the smaller number seeing what makes ten and what is left over.</i></p>	<p>$6 + 6 = 12$ Make 9 in one and 3 in the other. Take one from the 3 to make the 9 into a ten....$10 + 2 = 12$</p>  <p>Regrouping to make 10; using ten frames and counters/cubes or using Numicon.</p> <p>$6 + 5$</p> 	<p>Children to draw the ten frame and counters/cubes.</p> 	<p>Children to develop an understanding of equality e.g.</p> <p>$6 + \square = 11$ $6 + 5 = 5 + \square$ $6 + 5 = \square + 4$</p>

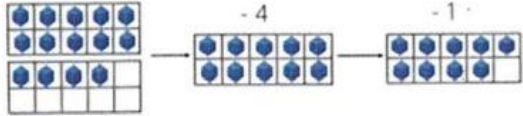
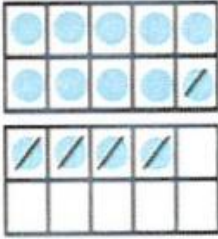
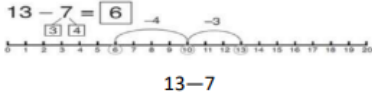
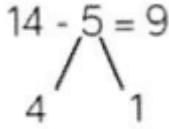


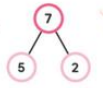
Year 1 Subtraction

Part, whole, subtraction, subtract, take away, distance between, difference between, more than, minus, less than, equals =, same as, most, least, pattern, odd, even, digit,

Concrete		Pictorial	Abstract
<p>Taking away should begin with physical objects: toys, cubes, Dienes etc They should be physically taken away and removed from the whole.</p>	<p>Ten frames Numicon Cubes Toys</p> <p>$6 - 3 = 3$</p>  <p>$4 - 3 = 1$</p>  <p>When subtracting using Dienes children should be taught to regroup a ten rod for</p>	<p>Children draw the concrete resources and cross them out. The bar model can also be used.</p> 	<p>$7 - 4 =$ $16 - 9 =$</p> <p>$4 - 3 =$</p> 

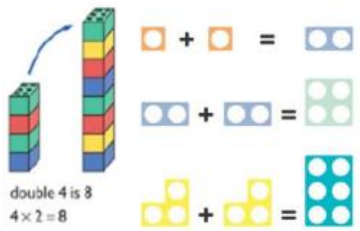

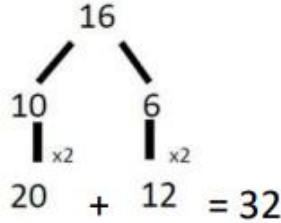
Concrete	Pictorial	Abstract
<p data-bbox="315 172 808 279">10 ones and then subtract from those ones $20 - 4 = 16$</p>  <p>The concrete representation shows two groups of ten. The first group consists of two green sticks. The second group consists of one green stick and ten yellow beads. The second group is then shown with four yellow beads removed, leaving one green stick and six yellow beads, representing the result of the subtraction.</p>	<p data-bbox="927 209 1413 272">Cross out drawn objects to show what has been taken away.</p>  <p>The pictorial representation shows two groups of triangles. The first group is a pyramid of 15 triangles (3 rows of 3). The second group is a smaller pyramid of 3 triangles (2 rows of 2, with 1 triangle below). The second group is crossed out with diagonal lines, representing the subtraction of 3 from 15.</p> <p data-bbox="972 512 1173 552">$15 - 3 = 12$</p>	

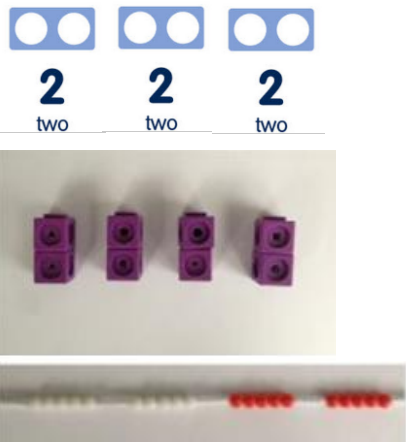
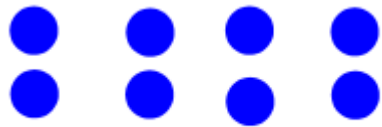
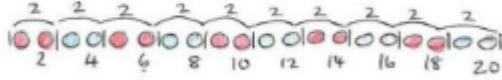
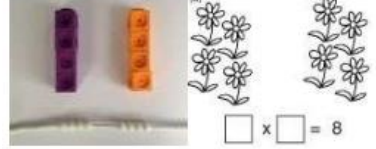

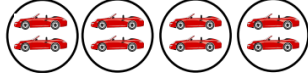
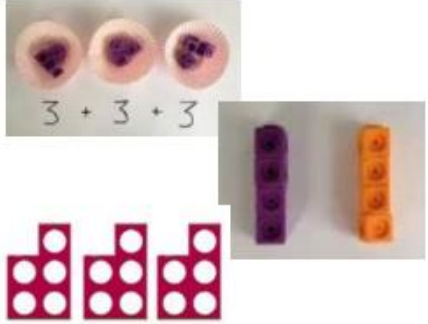


	Concrete	Pictorial	Abstract
<p>Subtraction by counting back</p> <p>Subtracting a single digit number from a single digit number and a single digit from a two digit by crossing out pictures</p>	<p>Counting back (using number lines or number tracks) children start with 6 and count back 2.</p> <p>$6 - 2 = 4$</p>   <p>Move the beads along the bead string as you count backwards.</p>	<p>Let's Learn</p> <p>Subtract by Counting Back</p> <p>Count back 3 steps from 15.</p> <p>Subtract 3 from 15.</p>  <p>$15 - 3 = 12$</p> <p>There are 12 flowers left.</p> <p>Children to represent what they see pictorially e.g.</p>  <p>Subtract by Crossing Out</p>  <p>$7 - 2 = 5$</p> <p>5 ladybirds are left.</p>	<p>Children to represent the calculation on a number line or number track and show their jumps. Encourage children to use an empty number line</p>   <p>Put 13 in your head, count back 4. What number are you at?</p>
<p>Finding the difference</p>	<p>Cubes, numicon or cuisenaire rods. Calculate the difference between 8 and 5.</p>  <p>Lay objects to represent bar model.</p>	<p>Draw the cubes they have used and show difference.</p> <p>Use bar models to show difference.</p> 	<p>Find the difference between 8 and 5. $8 - 5$, the difference is []</p> <p>Children to explore why $9 - 6 = 8 - 5 = 7 - 4$ have the same difference.</p> <p>Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?</p>

	Concrete	Pictorial	Abstract
Making 10 (partitioning numbers)	Using ten frames $14 - 5 = 14 - 4$ then $- 1$ 	Draw ten frames and discuss what they did to make 10.  $13 - 7 = \boxed{6}$  $13 - 7$ Jump back 3 first, then another 4. Use ten as the stopping point.	Children show how they can make 10 by partitioning the subtrahend. $14 - 4 = 10$ $10 - 1 = 9$  $14 - 5 = 9$ 4 1
Subtracting using the part part whole (include problem solving with missing digits).	If there are 7 cubes and 4 are purple, how many are not purple? 	 $7 - 5 = 2$ 2 boats are not red. How many boats are not red? 	$? - 5 = 2$

Year 1 Multiplication

Part, whole, ones, groups, lots of, multiply, multiplication, equal, same size, doubling, repeated addition, groups of, times, odd, even, columns, rows, X times longer, bigger, higher etc,

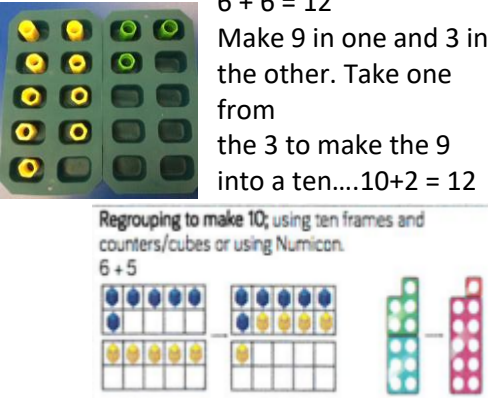
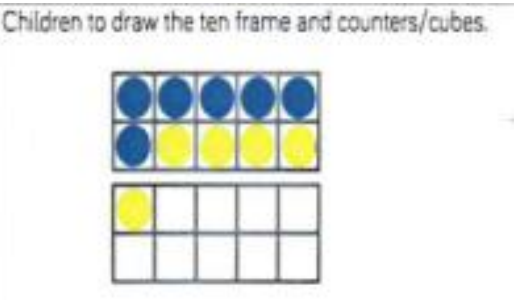

	Concrete	Pictorial	Abstract
Doubling	Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling  $4 \times 2 = 8$ $4 + 4 = 8$	Draw pictures to show how to double numbers Double 4 is 8 	Partition a number and then double each part before recombining it back together.  16 10 6 $\times 2$ $\times 2$ 20 12 $20 + 12 = 32$

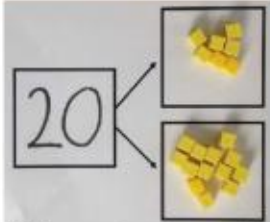
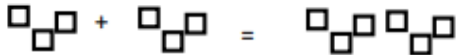
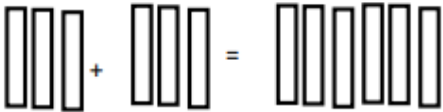
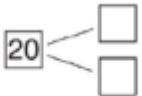


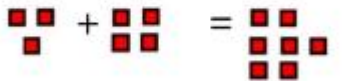
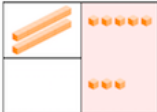
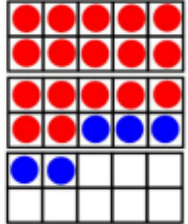
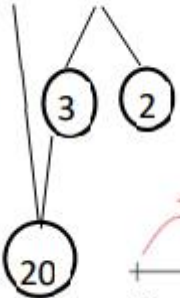
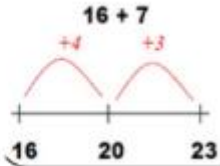
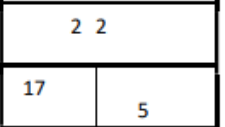
	Concrete	Pictorial	Abstract
<p>Counting in multiples of 2, 5 and 10 from zero <i>Children should count the number of groups on their fingers as they are skip counting.</i></p>	 <p>2 two 2 two 2 two</p>	<p>② ④ ⑥ ⑧ 4 groups of 2 = 8</p>  <p>Children make representations to show counting in multiples.</p> 	<p>Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30</p>
<p>Making equal groups and counting the total</p>	 <p>□ x □ = 8</p> <p>Use manipulatives to create equal groups.</p>	<p>Draw  to show 2 x 3 = 6</p>  <p>Draw and make representations</p>	<p>4 x 2 = 8 3 x 5 = 15 7 x 10 = 70</p>
<p>Solving multiplication problems using repeated addition involving 2s, 5s and 10s.</p>	 <p>3 + 3 + 3</p> <p>Use different objects to add equal groups</p>	<p>Use pictorial including number lines to solve prob There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p>  <p>How many apples are there altogether? 3 + 3 + 3 = 9</p> <p>3 + 3 + 3 + 3 + 3 = 15</p>	<p>Write addition sentences to describe objects and pictures.</p>  <p>2 + 2 + 2 + 2 + 2 = 10</p>


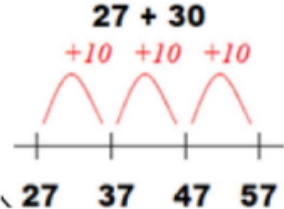

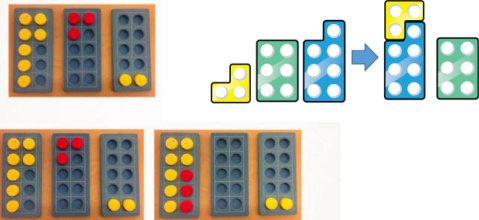

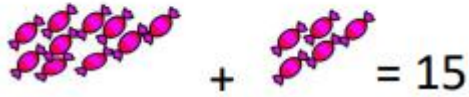
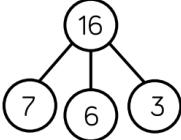
Year 2 Addition

Add, addition, more than, plus, altogether, sum, total, make, increase, partition, inverse, greatest, how many more to make?, ones, tens, tens boundary, one more, ten more, increase, partition, inverse, smallest, exchange, is the same as/ equal to, =, part part whole

	Concrete	Pictorial	Abstract													
<p>Learn number bonds to 20 and demonstrate related facts <i>Teach addition and subtraction alongside each other as pupils need to see the relationship between the facts.</i></p>	<div data-bbox="309 411 741 683"> $5 = 3 + 2$ $5 = 2 + 3$ <hr/> $5 - 3 = 2$ $5 - 2 = 3$ </div> <div data-bbox="324 703 779 817"> </div> <div data-bbox="309 842 472 874"> <p>2 more than 5.</p> </div> <div data-bbox="555 858 786 1114"> <table border="1"> <tr><td>●</td><td>●</td></tr> <tr><td>●</td><td>●</td></tr> <tr><td>●</td><td>●</td></tr> <tr><td>●</td><td>●</td></tr> <tr><td>●</td><td>●</td></tr> </table> <p>6 + 4 = 10 4 + 6 = 10 10 - 4 = 6 10 - 6 = 4</p> <p>Tens Frame</p> </div>	●	●	●	●	●	●	●	●	●	●	<div data-bbox="808 411 1339 619"> </div> <div data-bbox="846 879 1115 1034"> $6 + 4 = 10$ $4 + 6 = 10$ $10 - 4 = 6$ $10 - 6 = 4$ </div>	<div data-bbox="1480 416 1653 703"> $8 + 4 = 12$ $4 + 8 = 12$ </div> <div data-bbox="1832 523 2123 603"> <p>This is a family of addition and subtraction facts.</p> </div> <div data-bbox="1854 651 2101 703"> $12 - 8 = 4$ $12 - 4 = 8$ </div> <div data-bbox="1704 746 2101 778"> <p>Include missing number questions:</p> </div> <div data-bbox="1704 826 1877 863"> $8 = ? + 3$ </div> <div data-bbox="1704 895 1877 932"> $5 + ? = 8$ </div> <div data-bbox="1480 863 1697 943"> <table border="1"> <tr><td>10</td></tr> <tr><td>6</td><td>4</td></tr> </table> </div> <div data-bbox="1541 991 1653 1098"> $6 + 4 = 10$ $4 + 6 = 10$ $10 - 4 = 6$ $10 - 6 = 4$ </div> <div data-bbox="1742 991 2145 1023"> <p>Emphasis should be on the language</p> </div> <div data-bbox="1742 1050 2056 1177"> <p>'1 more than 5 is equal to 6.' '2 more than 5 is 7.' '8 is 3 more than 5.'</p> </div>	10	6	4
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	Concrete	Pictorial	Abstract
<p>Bridging 10 Use ten frames, Singapore bars, egg boxes and number lines to practice. <i>Chn should start with the larger number and add the smaller number seeing what makes ten and what is left over.</i></p>	<p>$6 + 6 = 12$ Make 9 in one and 3 in the other. Take one from the 3 to make the 9 into a ten....$10 + 2 = 12$</p> <p>Regrouping to make 10; using ten frames and counters/cubes or using Numicon. $6 + 5$</p> 	<p>Children to draw the ten frame and counters/cubes.</p> 	<p>Children to develop an understanding of equality e.g.</p> <p>$6 + \square = 11$ $6 + 5 = 5 + \square$ $6 + 5 = \square + 4$</p>
<p>Adding multiples of ten</p>	<p>$50 = 30 + 20$</p>  <p>Model using dienes and bead strings</p>	 <p>3 tens + 5 tens = _____ tens $30 + 50 = \underline{\hspace{2cm}}$</p> <p>Use representations for base ten.</p>	<p>$20 + 30 = 50$ $70 = 50 + 20$ $40 + \square = 60$</p>

	Concrete	Pictorial	Abstract												
Using known facts	 <p>Children explore ways of making numbers within 20</p>  	 $\square + \square = 20 \quad 20 - \square = \square$ $\square + \square = 20 \quad 20 - \square = \square$    <p>Children draw representations of H,T and O</p>	<p>Explore commutativity of addition by swapping the addends to build a fact family. Explore the concept of the inverse relationship of addition and subtractions and use this to check calculations.</p> $\square + 1 = 16 \quad 16 - 1 = \square$ $1 + \square = 16 \quad 16 - \square = 1$ <p>3+4=7 Leads to 30+40=70 Leads to 300+400=700</p>												
Add a 2 digit number with a 1 digit number.	<p>25 + 3</p>   <p>17 + 5 = 22 Use ten frame to make 'magic ten'</p> <p>Children explore the pattern.</p> $17 + 5 = 22$ $27 + 5 = 32$	<p>17 + 5 = 22</p> <p>Use part part whole and number line to model.</p>  	<p>17 + 5 = 22</p> <p>Explore related facts</p> $17 + 5 = 22$ $5 + 17 = 22$ $22 - 17 = 5$ $22 - 5 = 17$  <p>Lead into recording in column format, to reinforce place value and prepare children for formal written methods with larger values.</p> <table border="1" data-bbox="1944 1066 2145 1225"> <thead> <tr> <th></th> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td></td> <td>2</td> <td>5</td> </tr> <tr> <td>+</td> <td></td> <td>3</td> </tr> <tr> <td colspan="2"><hr/></td> <td>8</td> </tr> </tbody> </table>		tens	ones		2	5	+		3	<hr/>		8
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	Concrete	Pictorial	Abstract
Add a 2 digit number and 10s number.	 <p>$25 + 10 = 35$</p> <p>Explore that the ones digit does not change</p>	 <p>$27 + 30$</p> <p>$+10 +10 +10$</p> <p>27 37 47 57</p>	<p>$27 + 10 = 37$</p> <p>$27 + 20 = 47$</p> <p>$27 + \square = 57$</p>
Add three 1 digit numbers.	 <p>Combine to make 10 first if possible, or bridge 10 then add third digit</p> <hr/> <p>$7 + 3 + 2 =$ leads to $10 + 2 =$</p> 	 <p>Regroup and draw representation.</p>  <p>$= 15$</p>	<p>$(4 + 7 + 6) = 10 + 7$</p> <p>10</p> <p>$= 17$</p> <p>Combine the two numbers that make/bridge ten then add on the third.</p> 

Concrete

Add two 2 digit numbers.

use place value counters and dienes to model this.

Step 1 Add the ones.

tens	ones
1	9
+ 2	0
<hr/>	
	9

Step 2 Add the tens.
1 ten + 2 tens = 3 tens

tens	ones
1	9
+ 2	0
<hr/>	
3	9

19 + 20 = 39

Tens	Ones
10 10 10	1 1 1 1 1
10 10	1 1 1
10	

Pictorial

Draw the ten sticks and ones dots
Draw place value counters.
Use a number line.

Partitioning method

$$\begin{array}{l} 25 + 47 \\ \swarrow \quad \searrow \\ 20 + 5 \quad 40 + 7 \end{array}$$

Children to represent the base 10 in a place value chart.

10s	1s
6	1

$$\begin{array}{l} 20 + 40 = 60 \\ 5 + 7 = 12 \\ 60 + 12 = 72 \end{array}$$

Abstract

Expanded column method

Add 15 and 18.

Use to help you add.

Step 1 Add the ones.
5 ones + 8 ones = 13 ones
Regroup the ones.
13 ones = 1 ten and 3 ones

tens	ones
1	5
+ 1	8
<hr/>	
1	3

Step 2 Add the tens.
1 ten + 1 ten + 1 ten = 3 tens

tens	ones
1	5
+ 1	8
<hr/>	
1	3
+ 2	0
<hr/>	
3	3

15 + 18 = 33

If/when ready move to column method or leave for Y3

tens	ones
1	9
+ 2	0
<hr/>	
	9

tens	ones
1	9
+ 2	0
<hr/>	
3	9

$$\begin{array}{r} 15 \\ +34 \\ \hline 49 \end{array}$$

Using the bar to find missing digits.

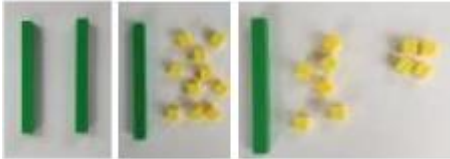

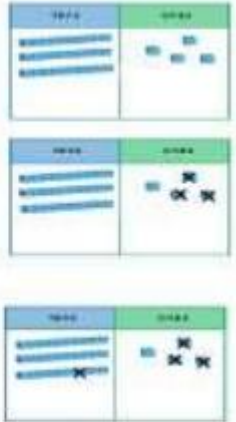

Use dienes, place value counters and Cuisenaire rods to build bar models.

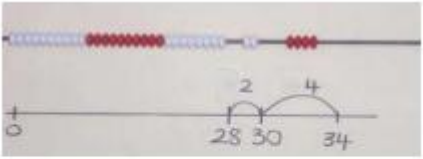
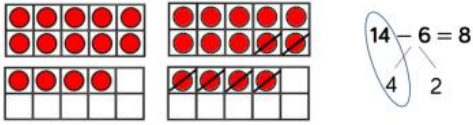
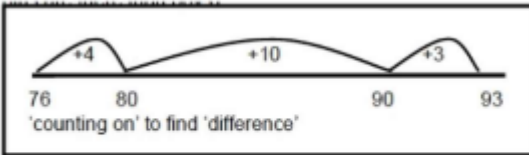
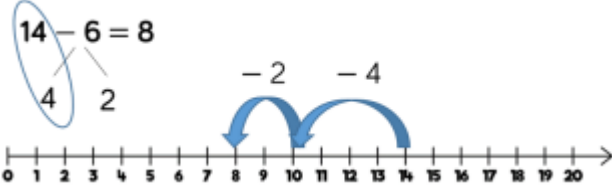


It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.

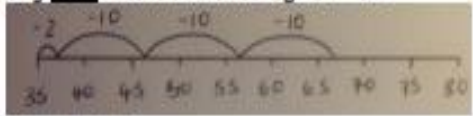
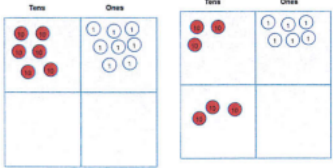
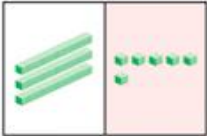
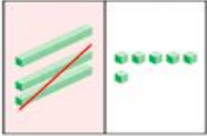
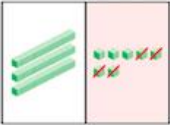
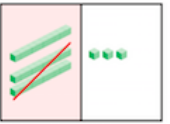
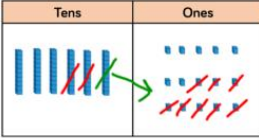
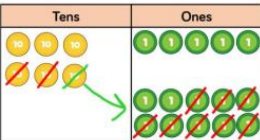
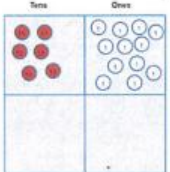
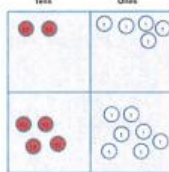
Helen has 14 breadsticks. Her friend has 17. How many do they have altogether?


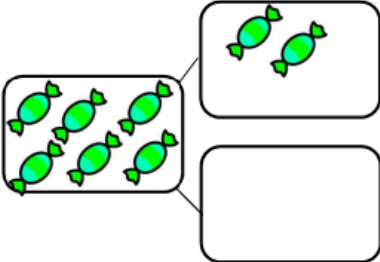
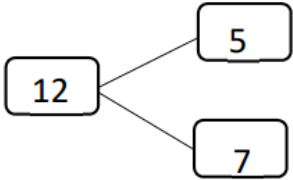
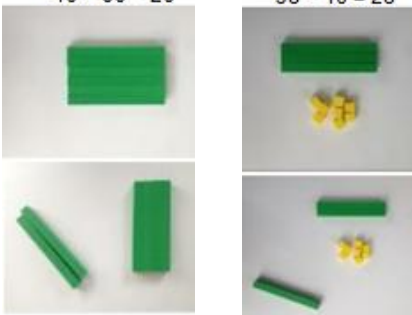
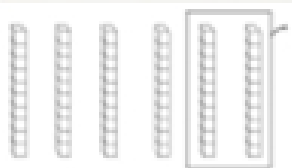
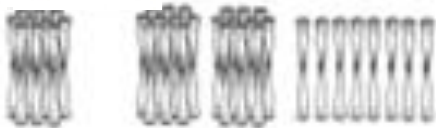
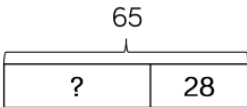
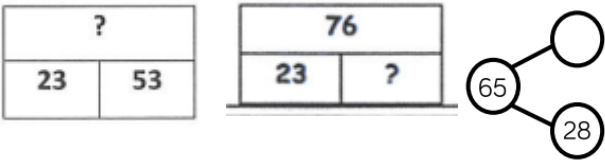
Year 2 Subtraction

subtract, subtraction, minus, take away, difference, less, inverse, decrease, greatest, smallest, fewer than., exchange, part-part whole, partition, one less than., ten less than.,

	Concrete	Pictorial	Abstract				
<p>Regroup/exchange a ten into ten ones</p>	 <p>Use a PV chart to show how to change a ten into ten ones, use the term 'take and make'</p>	 $20 - 4 =$	$25 - 9 = 16$				
<p>Partitioning to subtract without regrouping. 'Friendly numbers'</p>	<p>$34 - 13 = 21$</p>  <p>Use Dienes to show how to partition the number when subtracting without regrouping.</p>	<p>Children draw representations of Dienes and cross off.</p>  $43 - 21 = 22$ $\begin{array}{r} 46 - 25 = 21 \\ \textcircled{40} \textcircled{6} - \textcircled{20} \textcircled{5} \end{array}$ <table border="1" style="display: inline-table; margin-right: 20px;"> <tr> <td style="background-color: yellow;">t</td> <td style="background-color: pink;">o</td> </tr> <tr> <td> xx</td> <td> xx</td> </tr> </table> $6 - 5 = 1$ $40 - 20 = 20$ $20 + 1 = 21$ <p><i>(children must be taught to always start with the ones)</i></p>	t	o	xx	xx	$43 - 21 = 22$
t	o						
xx	xx						






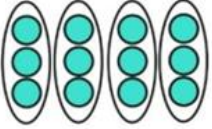
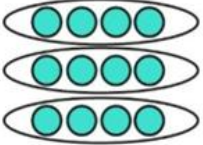


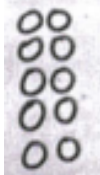



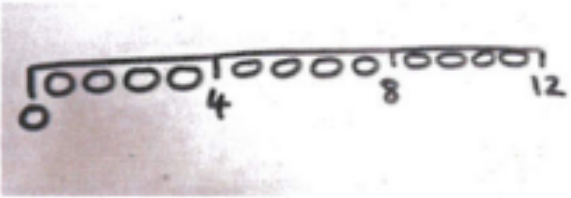

	Concrete	Pictorial	Abstract																																																														
<p>Make ten strategy – counting up to find the difference rather than subtract OR partition to get back to the ten then keep subtracting.</p>	<p>Concrete</p>  <p>$34 - 28$</p> <p>Use a bead bar or bead strings to model counting to next ten and the rest.</p> 	<p>Pictorial</p>  <p>'counting on' to find 'difference'</p> <p>Use a number line to count on to next ten and then the rest.</p> 	<p>Abstract</p> <p>$93 - 76 = 17$ (count up from 76 to 93)</p> <p>$85 - 73 = 12$ (Count back from 85 to 80 then back to 73. Add steps together)</p>																																																														
<p>Subtract a 1 digit number from 2 digit number.</p>	<p>Concrete</p> <p>Step 1 Subtract the ones. 8 ones - 3 ones = 5 ones</p>  <p>Step 2 Subtract the tens.</p>  <p>$28 - 3 = 25$</p> <p>48-7</p> <table border="1" data-bbox="327 1118 763 1265"> <tr> <th>10s</th> <th>1s</th> <th>10s</th> <th>1s</th> </tr> <tr> <td>4 rods</td> <td>8 units</td> <td>4 rods</td> <td>1 unit</td> </tr> </table>	10s	1s	10s	1s	4 rods	8 units	4 rods	1 unit	<p>Children to represent the base 10 pictorially.</p> <table border="1" data-bbox="842 751 1021 903"> <tr> <th>10s</th> <th>1s</th> </tr> <tr> <td>4 rods</td> <td>1 unit</td> </tr> </table>	10s	1s	4 rods	1 unit	<p>Start to set up the column subtractions to reinforce the place value of the digits Children can count back to find the answer also</p> <table border="0" data-bbox="1503 815 1939 983"> <tr> <td></td> <td>tens</td> <td>ones</td> <td></td> </tr> <tr> <td>-</td> <td>2</td> <td>8</td> <td></td> </tr> <tr> <td></td> <td></td> <td>3</td> <td></td> </tr> <tr> <td colspan="4"><hr/></td> </tr> <tr> <td></td> <td></td> <td>5</td> <td></td> </tr> <tr> <td colspan="4"><hr/></td> </tr> <tr> <td></td> <td>4</td> <td>1</td> <td></td> </tr> <tr> <td colspan="4"><hr/></td> </tr> </table> <table border="0" data-bbox="1503 983 1738 1118"> <tr> <td></td> <td>tens</td> <td>ones</td> </tr> <tr> <td>-</td> <td>2</td> <td>8</td> </tr> <tr> <td></td> <td></td> <td>3</td> </tr> <tr> <td colspan="3"><hr/></td> </tr> <tr> <td></td> <td>2</td> <td>5</td> </tr> <tr> <td colspan="3"><hr/></td> </tr> </table>		tens	ones		-	2	8				3		<hr/>						5		<hr/>					4	1		<hr/>					tens	ones	-	2	8			3	<hr/>				2	5	<hr/>		
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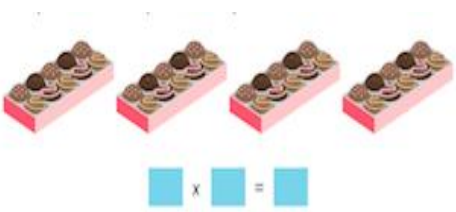
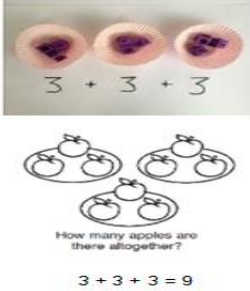
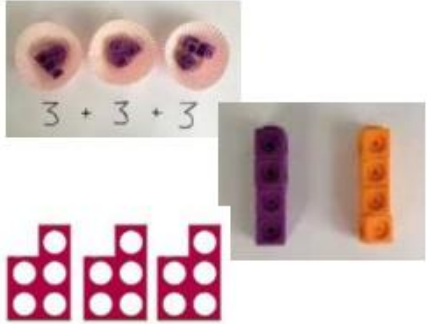
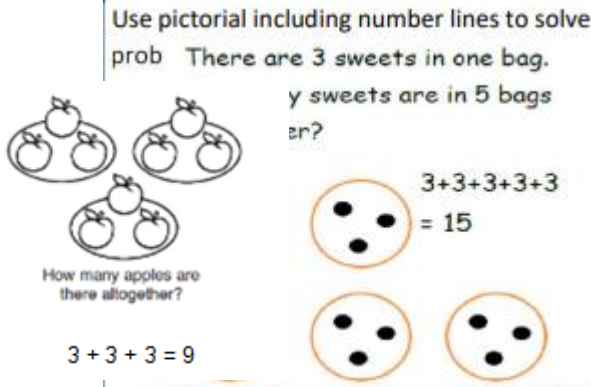

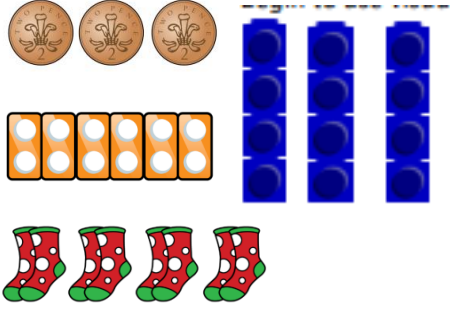
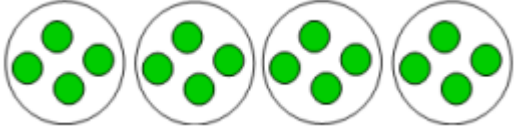
	Concrete	Pictorial	Abstract																																																				
<p>Subtract a 10s number from 2 digit number.</p>	<p>Counting back in 10's from the number on a numberline. Use place value counters and dienes and take the tens away. Notice the ones do not change.</p>  <p>68 - 30 =</p> 	<p>Children to represent the dienes pictorially and cross out</p> <p>Step 1 Subtract the ones.</p>  <table border="1" data-bbox="1182 276 1384 424"> <thead> <tr> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>6</td> </tr> <tr> <td>- 2</td> <td>0</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td>6</td> </tr> </tbody> </table> <p>Step 2 Subtract the tens. 3 tens - 2 tens = 1 ten</p>  <table border="1" data-bbox="1182 518 1384 667"> <thead> <tr> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>6</td> </tr> <tr> <td>- 2</td> <td>0</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td>1</td> <td>6</td> </tr> </tbody> </table> <p>36 - 20 = 16</p>	tens	ones	3	6	- 2	0	<hr/>			6	tens	ones	3	6	- 2	0	<hr/>		1	6	$\begin{array}{r} 68 \\ - 30 \\ \hline \end{array}$																																
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<p>Subtract a 2 digit number from 2 digit number (no exchanging needed)</p> <p>Greater depth to look at exchanging</p>	<p>Subtract 24 from 37.</p> <p>Step 1 Subtract the ones. 7 ones - 4 ones = 3 ones</p>  <table border="1" data-bbox="611 794 779 930"> <thead> <tr> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>7</td> </tr> <tr> <td>- 2</td> <td>4</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td>3</td> </tr> </tbody> </table> <p>Step 2 Subtract the tens. 3 tens - 2 tens = 1 ten</p>  <table border="1" data-bbox="611 986 779 1121"> <thead> <tr> <th>tens</th> <th>ones</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>7</td> </tr> <tr> <td>- 2</td> <td>4</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td>1</td> <td>3</td> </tr> </tbody> </table> <p>37 - 24 = 13</p>	tens	ones	3	7	- 2	4	<hr/>			3	tens	ones	3	7	- 2	4	<hr/>		1	3	<p>Children to represent the dienes pictorially and cross out</p>  <table border="1" data-bbox="1093 805 1171 914"> <tbody> <tr> <td>5</td> <td>6</td> </tr> <tr> <td>- 2</td> <td>8</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td>3</td> </tr> </tbody> </table>  <table border="1" data-bbox="1417 957 1473 1106"> <tbody> <tr> <td>7</td> <td>2</td> </tr> <tr> <td>- 4</td> <td>7</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table>	5	6	- 2	8	<hr/>			3	7	2	- 4	7	<hr/>				<p>Greater Depth:</p>  <table border="1" data-bbox="1709 1018 1765 1106"> <tbody> <tr> <td>7</td> <td>2</td> </tr> <tr> <td>- 4</td> <td>7</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table>  <table border="1" data-bbox="2022 1018 2078 1106"> <tbody> <tr> <td>7</td> <td>2</td> </tr> <tr> <td>- 4</td> <td>7</td> </tr> <tr> <td colspan="2"><hr/></td> </tr> <tr> <td></td> <td>5</td> </tr> </tbody> </table>	7	2	- 4	7	<hr/>				7	2	- 4	7	<hr/>			5
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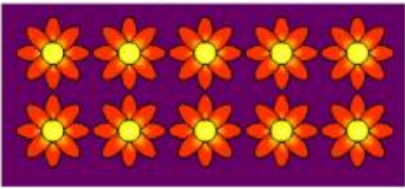
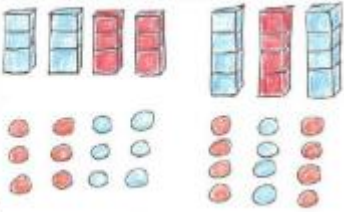

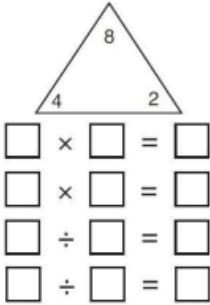
	Concrete	Pictorial	Abstract
<p>Represent and use number bonds and related subtraction facts within 20 Include subtracting zero Part Part Whole model</p>	 <p>Link to addition. Use PPW model to model the inverse.</p> <p>If 10 is the whole and 6 is one of the parts, what is the other part?</p> $10 - 6 = 4$	 <p>Use pictorial representations to show the part.</p>	<p>Move to using numbers within the part whole model.</p>  <p>Include missing number problems: $12 - ? = 5$ $7 = 12 - ?$</p>
<p>Subtracting multiples of 10</p> <p><i>Using the vocabulary of 1 ten, 2 tens etc alongside 10, 20, 30 is very important here as pupils need to understand that it is a 10 not a 1 that is being taken away</i></p>		<p>6 tens - 2 tens = [] tens</p> $60 - 20 =$  $38 - 10 =$ 	$80 - 30 =$ $50 = 70 - ?$ $36 - 10 =$
<p>Recognise and use the inverse relationship between addition and subtraction</p>	<p>Use dienes and place value counters</p> 		$23 + ? = 56$ $96 - ? = 48$ $65 = 41 + ?$

Year 2 Multiplication

lots of, groups of, repeat, times, multiply, multiplied by, multiple of, array, row, column, double, part, whole


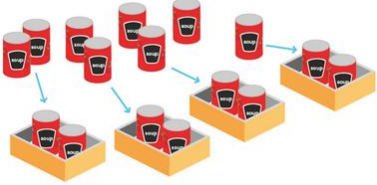


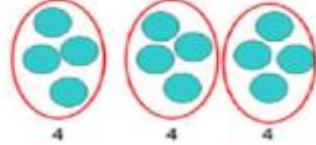

	Concrete	Pictorial	Abstract
<p>Multiplication is commutative</p> <p><i>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</i></p>	<p>Create arrays using counters and cubes and Numicon.</p>    <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p>  	<p>Pictorial</p>   <p>$12 = 3 \times 4$ $12 = 4 \times 3$</p> <p>How many dots are there?</p>   <p>$2 \times 5 = 10$ $5 \times 2 = 10$</p> <p>2×5 is equal to 5×2.</p>  	<p>Abstract</p> <p>$12 = 4 \times 3$ $12 = 3 \times 4$</p> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p>$5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$</p>
<p>Recall and use multiplication facts for the multiplication tables 2, 5 and 10.</p>	 <p> $1 \times 5 = 5$ $2 \times 5 = 10$ $3 \times 5 = 15$ $4 \times 5 = 20$ $5 \times 5 = 25$ $6 \times 5 = 30$ $7 \times 5 = 35$ $8 \times 5 = 40$ $9 \times 5 = 45$ $10 \times 5 = 50$ </p>	<p>3×4</p> 	<p>3×4</p> 


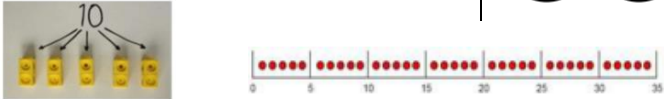

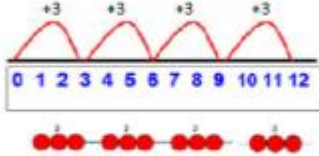
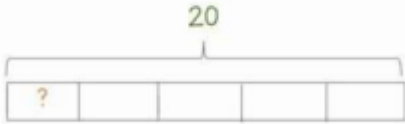
	Concrete	Pictorial	Abstract
<p>I can use multiplication (x) and equal (=) sign when writing out my times tables.</p>			
<p>Solving multiplication problems using repeated addition.</p>	 <p>Use different objects to add equal groups</p>	<p>Use pictorial including number lines to solve prob There are 3 sweets in one bag. y sweets are in 5 bags er?</p>  <p>How many apples are there altogether?</p> <p>$3 + 3 + 3 = 9$</p>	<p>Write addition sentences to describe objects and pictures.</p>  <p>$2 + 2 + 2 + 2 + 2 = 10$</p>
<p>Grouping Begin to use visual and concrete apparatus to find the answers to '3 lots of 4' or '2 lots of 5' etc</p>		<p>Drawing 4 lots of 4 to find a whole</p> 	<p>6 lots of 2 =</p> <p>4 groups of 5 =</p>

	Concrete	Pictorial	Abstract
<p>Understanding arrays - show that multiplication of two numbers can be done in any way (commutative)</p>	<p>Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.</p> 	<p>Draw representations of arrays to show understanding</p> 	<p>$3 \times 2 = 6$</p> <p>$2 \times 5 = 10$</p>
<p>Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.</p>	<p>$4 \times 2 = 8$ $8 \div 4 = 2$</p> 	<p>Fact Families</p> 	<p>$2 \times 4 = 8$ $4 \times 2 = 8$ $8 \div 2 = 4$ $8 \div 4 = 2$ $8 = 2 \times 4$ $8 = 4 \times 2$ $2 = 8 \div 4$ $4 = 8 \div 2$</p> <p>Show all 8 related fact family sentences.</p>

Year 2 Division

divided by, divided into, sharing, into groups, halve, share, one each... two each... three each etc., left over, how many groups? Part, whole, equal groups, remainder

	Concrete	Pictorial	Abstract
<p>Sharing - Pupils should be taught to divide through working practically and the sharing should be shown below the whole to familiarize children with the concept of the whole.</p> <p><i>The language of whole and part part should be used.</i></p>	<p>I have 10 cubes, can you share them equally in 2 groups?</p>  <p>1 There are 8 cans.</p>  <p>There are 4 boxes of 2 cans.</p>	<p>I have 10 strawberries and share them with my friend. How many do we have each?</p>  <p>Children use pictures or shapes to share equally</p>  <p>8 shared between 2 is 4</p> <p>Sharing:</p>  <p>12 shared between 3 is 4</p> <p>Children use bar modelling to show and support understanding.</p>  <p>12 ÷ 4 = 3</p>	<p><i>The division symbol is not formally taught at this stage but it can be introduced.</i></p> <p>8 shared between 4 = 2 $12 \div 4 = 3$</p> <div style="border: 1px solid black; padding: 10px; margin: 20px auto; width: fit-content;"> <p>Division should be taught through the use of stories and real life problems.</p> </div>

	Concrete	Pictorial	Abstract
<p>Grouping - into equal groups to divide by 2, 5 and 10.</p>	<p>15 balls put into 5 bags</p>  	<p>15 balls put into 5 bags</p>  <p>Use number lines for grouping</p>  <p>$12 \div 3 = 4$</p> <p>Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.</p>  <p>$20 \div 5 = ?$ $5 \times ? = 20$</p>	



	Concrete	Pictorial	Abstract
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Division as grouping


Start looking at remainders and how they are not all equal groups

Use cubes, counters, objects or place value counters to aid understanding.

Put 10 buns in groups of 2.
How many plates are there?

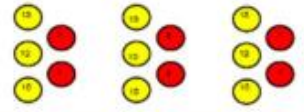



Put into groups of 5.
There are groups.




24 divided into groups of 6 = 4

$96 \div 3 = 32$

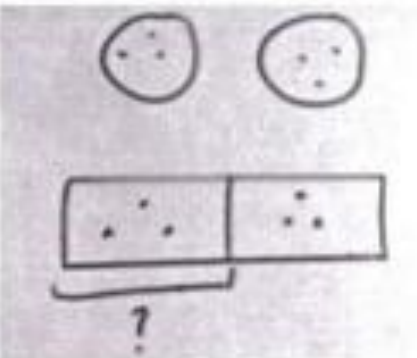
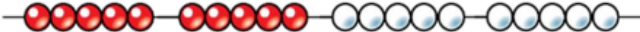


Continue to use bar modelling to aid solving division problems.

20

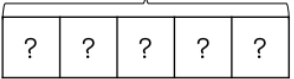


$20 \div 5 = ?$
 $5 \times ? = 20$

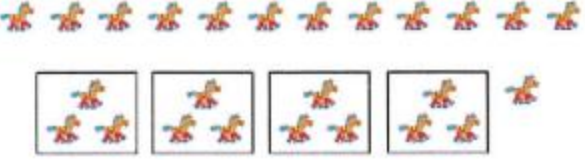



How many groups of 6 in 24?
 $24 \div 6 = 4$

20



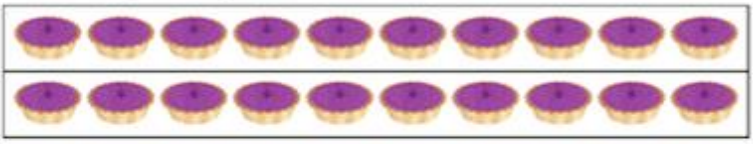
Greater Depth with remainders



$13 \div 4 = 3 \text{ Remainder } 1$

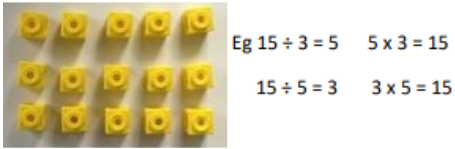
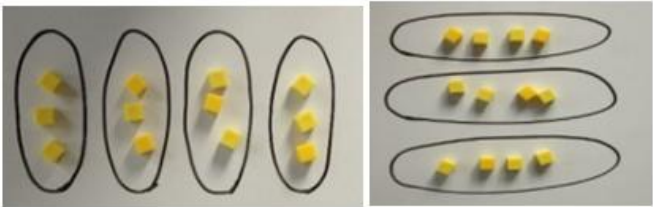
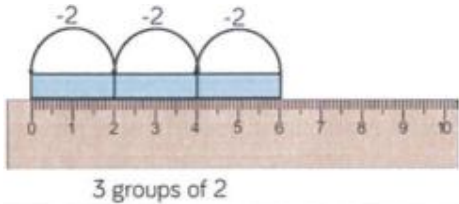
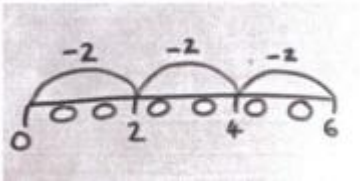
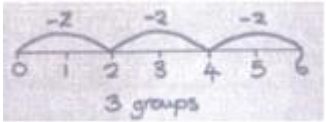
Recall and use division facts for the multiplicatio


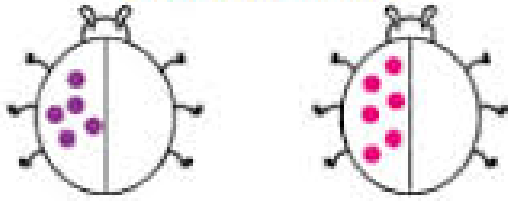
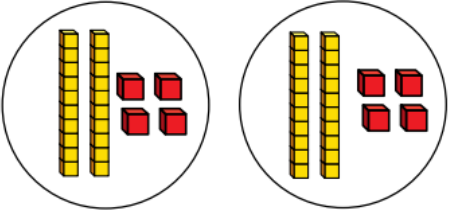
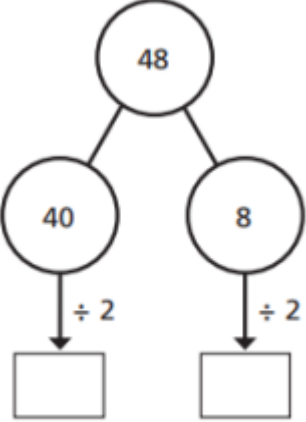
Make a family of multiplication and division facts.



$2 \times 10 = 20$ ————— $20 \div 10 =$

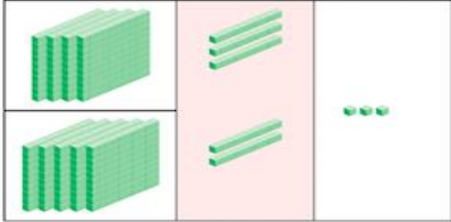
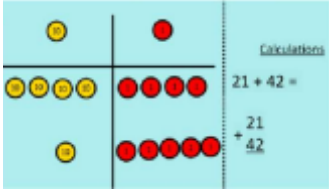
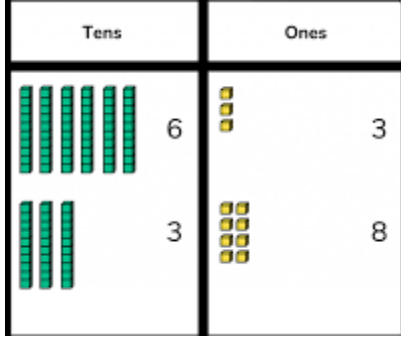
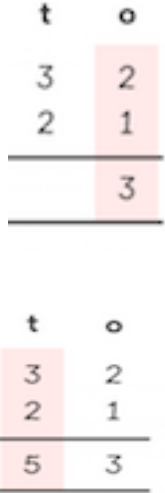
$10 \times 2 = 20$ ————— $20 \div 2 =$

	Concrete	Pictorial	Abstract
n tables 2, 5 and 10.			
Solve division problems in context using arrays	<p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> 	<p>Children draw the total into rows and see how many columns they have.</p> 	<p>Find the inverse of multiplication and division sentences by creating eight linking number sentences.</p> $7 \times 4 = 28 \quad 4 \times 7 = 28 \quad 28 \div 7 = 4 \quad 28 \div 4 = 7$ $28 = 7 \times 4 \quad 28 = 4 \times 7 \quad 4 = 28 \div 7 \quad 7 = 28 \div 4$
I can use the inverse.	This should be taught alongside both multiplication and division.		
Division as repeated subtractions			

	Concrete	Pictorial	Abstract						
To know halves to 24	 <p>The concrete representation shows a green ten-frame divided into two halves, each containing five dots. Below it, base ten blocks are used to represent the number 24, with two tens rods and four ones units.</p>	 <p>The pictorial representation shows two ladybugs. The first ladybug has 12 purple spots on its back, and the second ladybug has 12 pink spots. Each ladybug is divided into two halves, representing halves of 24.</p>	$14 \div 2 = 7$						
To divide 2 digits by 1 digit numbers	<p>$48 \div 2 = 24$</p> <table border="1" data-bbox="338 762 772 943"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td>10 10</td> <td>1 1 1 1</td> </tr> <tr> <td>10 10</td> <td>1 1 1 1</td> </tr> </tbody> </table>  <p>The concrete representation shows two circles. Each circle contains two tens rods (yellow) and four ones units (red), representing the number 48.</p>	Tens	Ones	10 10	1 1 1 1	10 10	1 1 1 1	 <p>The pictorial representation shows a tree diagram. The root node is 48. It branches into two nodes: 40 and 8. Below each node is a downward arrow with a division symbol and the number 2, pointing to an empty square box.</p>	$48 \div 2 = 24$
Tens	Ones								
10 10	1 1 1 1								
10 10	1 1 1 1								

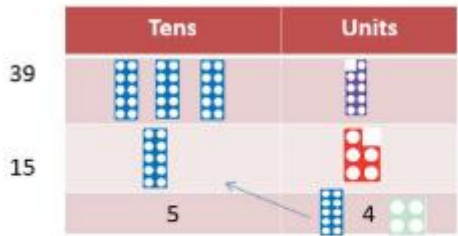
Year 3 Addition

Addends, add, addition, plus, and, altogether, more, sum, total, increase, number line, count on, partition, recombine, estimate, inverse, how many more to make? How many more is ___ than ___? Hundreds, tens, ones, column method, part, whole, doubles, near doubles,

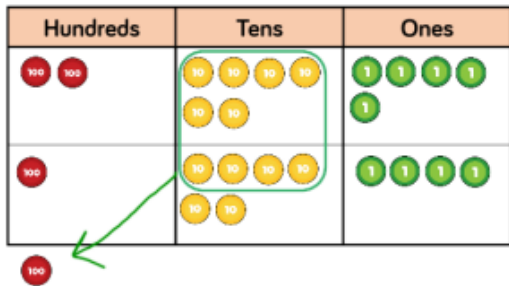
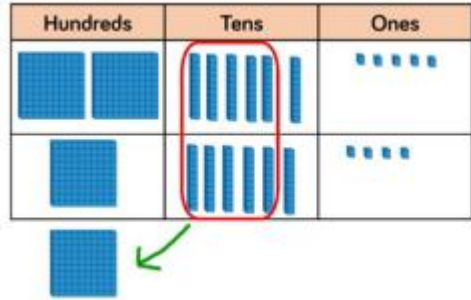
	Concrete	Pictorial	Abstract
<p>Add two two-digit numbers.</p> <p>Column Addition—no exchanging (friendly numbers)</p>	<p>Step 2 Add the tens. 3 tens + 2 tens = 5 tens</p>  <p>Move to using place value counters and 2 digit numbers.</p> 	<p>Children start to draw the dienes in the column method</p> 	<p>$32 + 21 =$</p> 

Column Addition with exchanging.

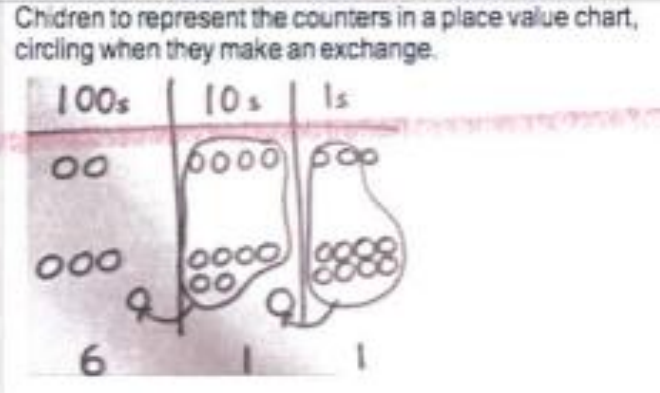
Concrete



Exchange ten ones for a ten. Model using numicon and place value counters.



Pictorial

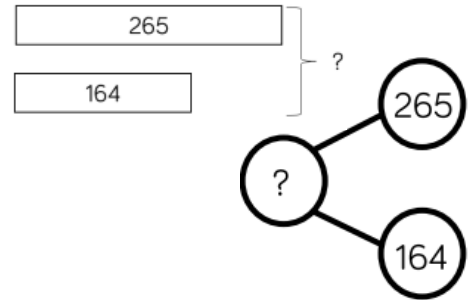


Abstract

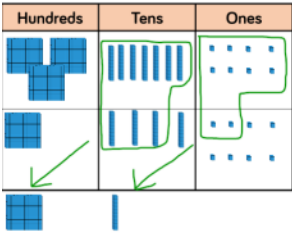
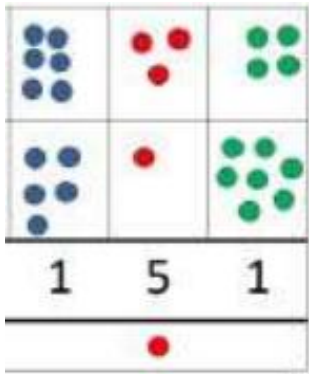
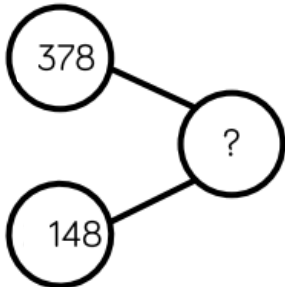
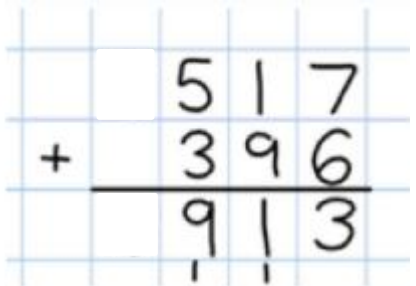


$$\begin{array}{r} 20 + 5 \\ 40 + 8 \\ \hline 60 + 13 = 73 \end{array}$$


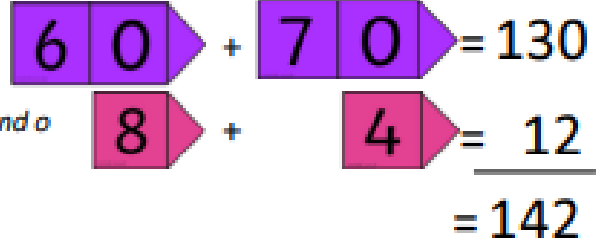

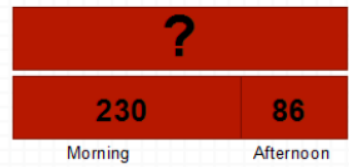
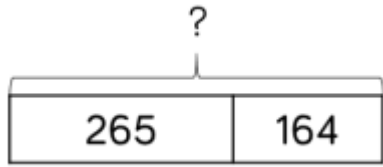
Start by partitioning the numbers before formal column to show the exchange.

$$\begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$$



	h	t	o
	2	8	7
+	1	0	5
	<hr/>	<hr/>	<hr/>
	3	9	2
		<hr/>	
		1	

	Concrete	Pictorial	Abstract
<p>Adding numbers with up to 3 digits.</p> <p><i>Again this should start with the children using dienes to support them with lots of discussion about the value of each digit.</i></p>	<p>Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand</p> 	<p>Pictorial</p>  	<p>Abstract</p> $\begin{array}{r} 3 \ 1 \ 4 \\ 2 \ 4 \ 0 \\ \hline 5 \ 5 \ 4 \end{array}$ <p>Step 1 Add the ones. 4 ones + 0 ones = 4 ones</p> <p>Step 2 Add the tens. 1 tens + 4 tens = 5 tens</p> <p>Step 3 Add the hundreds. 3 hundreds + 2 hundreds = 5 hundreds</p>  <p>Continue from previous work to carry hundreds as well as tens.</p> <p>Relate to money and measures.</p>
<p>Estimate the answers to questions and use inverse operations to check answers</p>	 <p>Estimating $98 + 17 = ?$ $100 + 20 = 120$</p>	<p>Use number lines to illustrate estimation.</p> 	<p>Building up known facts and using them to illustrate the inverse and to check answers:</p> <p>$98 + 18 = 116$ $116 - 18 = 98$ $18 + 98 = 116$ $116 - 98 = 18$</p>

	Concrete	Pictorial	Abstract
Mental addition skills	<p>Using place value <i>Count in hundreds eg. knowing 475+200 as 475, 575, 675</i> <i>Add multiples of 10, 100 and £1 eg. 746+200 or 746+40</i></p> <p><i>68 + 74 as 60 + 70 and 8 + 4, combining the two totals.</i></p> <p>Counting on <i>Add a three-digit and two-digit numbers by adding h, t and o</i> <i>eg. 125 + 34 as 100 + 20 + 30 + 5 + 4</i> <i>Add near multiples of 10 and 100</i> <i>eg. 67 + 39 as (67 + 40) - 1</i></p> <p>Using number facts <i>Number bonds to 100 eg. 65 + 35, 47 + 53, 71 + 29 etc.</i> <i>Adjustment when adding 9 and 11 eg. 27 + 9 as (27 + 10) - 1 or 36 + 11 as (36 + 10) + 1</i></p>	 	
Using the bar to find missing digits.	<p>Bar Model to support understanding of problem solving:</p>  <p>A man sold 230 balloons at a carnival in the morning. He sold another 86 balloons in the evening . How many balloons did he sell in all?</p>		

Year 3 Subtraction

subtract, subtraction, take away, less, minus, how many are left/left over? Inverse, decrease, difference, fewer than, more than, hundreds, tens, ones, boundary, how much less is ___ than ___? Column method, part, whole, partition, recombine. **Borrowing should not be used as a term because it implies that the borrowed number needs to go back.**

Subtract up to 3 digits from 3 digits.

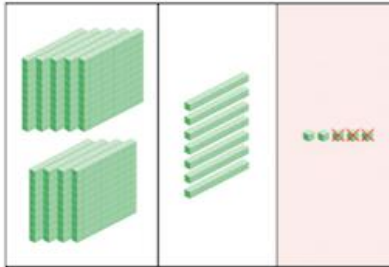
Very important for children to use dienes equipment along with a place value chart to support.

Only when secure with the method should exchanging be introduced.

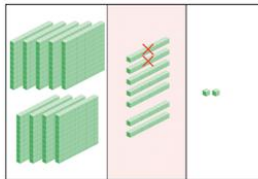
Concrete

Subtract 723 from 975.

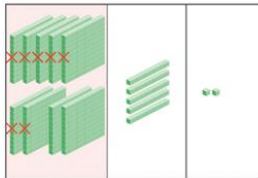
Step 1 Subtract the ones.
5 ones - 3 ones = 2 ones



Step 2 Subtract the tens.
7 tens - 2 tens = 5 tens

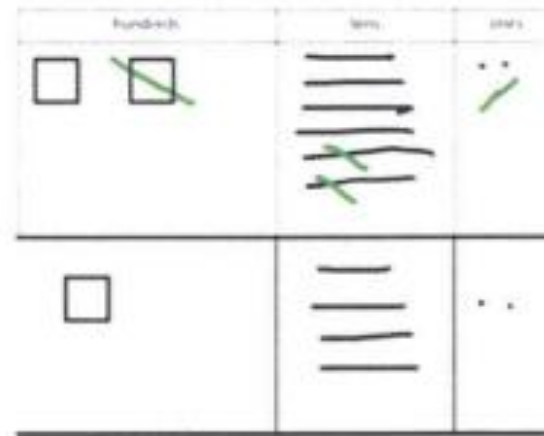


Step 3 Subtract the hundreds.
9 hundreds - 7 hundreds = 2 hundreds



$$975 - 723 = 252$$

Pictorial



$$263 - 121 = 142$$

Abstract

	h	t	o
	9	7	5
-	7	2	3
<hr/>			2

	h	t	o
	9	7	5
-	7	2	3
<hr/>			5 2

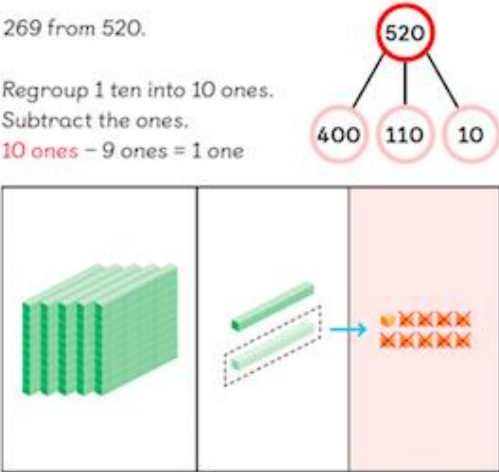
	h	t	o
	9	7	5
-	7	2	3
<hr/>			2 5 2

Subtract up to 3 digits from 3 digits with exchanging

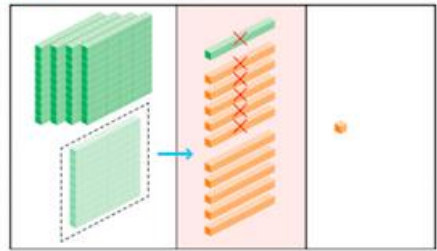
Concrete

Subtract 269 from 520.

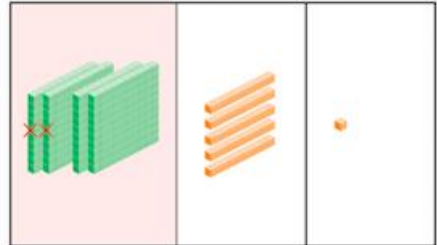
Step 1 Regroup 1 ten into 10 ones. Subtract the ones.
 $10 \text{ ones} - 9 \text{ ones} = 1 \text{ one}$



Step 2 Regroup 1 hundred into 10 tens. Subtract the tens.
 $11 \text{ tens} - 6 \text{ tens} = 5 \text{ tens}$

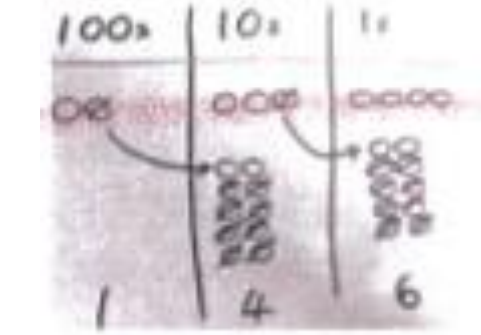


Step 3 Subtract the hundreds.
 $4 \text{ hundreds} - 2 \text{ hundreds} = 2 \text{ hundreds}$



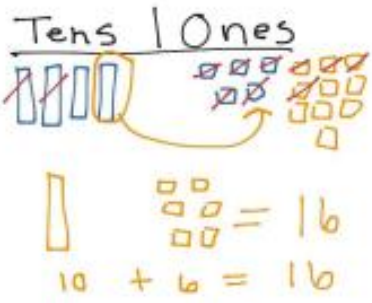
$520 - 269 = 251$

Pictorial



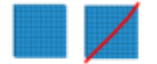


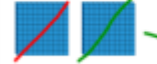


45
 -29
 16

Tens | Ones



$10 + 6 = 16$

Children may draw base ten or PV counters and cross off.

Hundreds	Tens	Ones
		
		

Abstract

$$836 - 254 = 582$$

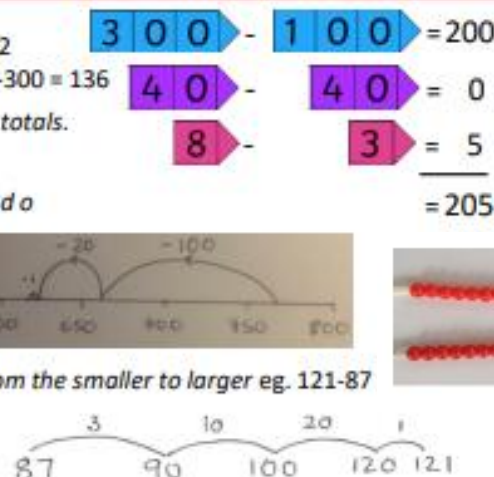

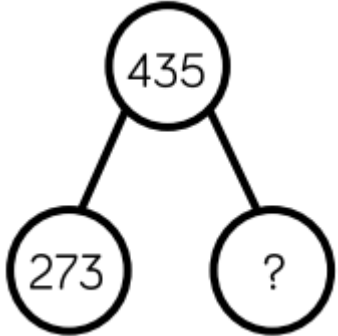
Begin by partitioning into pv columns

$$728 - 582 = 146$$

Then move to formal method.

	h	t	o
	5	2	10
-	2	6	9
<hr/>			
		5	1

	h	t	o
	4 5	2 ¹¹	10
-	2	6	9
<hr/>			
	2	5	1

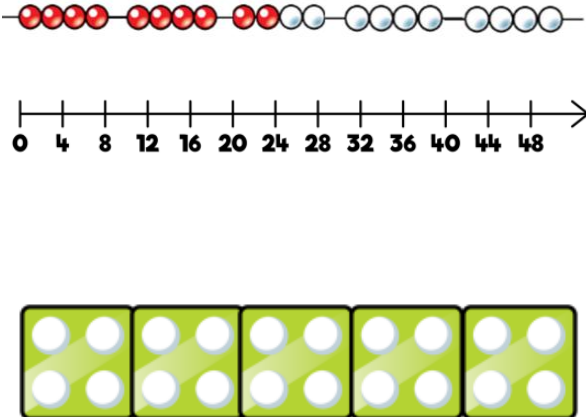
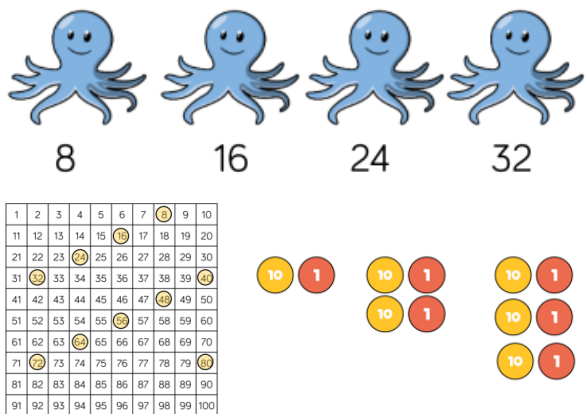
	Concrete	Pictorial	Abstract															
Subtract numbers mentally, including: three digit number - ones three digit number - tens three digit number - hundreds	<p>Using place value <i>Count back in hundreds eg. knowing 372-200 as 372, 272, 172</i> <i>Subtract multiples of 10, 100 and £1 eg. 476-40 = 436 or 436-300 = 136</i> <i>348 - 143 as 300 - 100, 40 - 40 and 8 - 3, combining the three totals.</i></p> <p>Counting back <i>Subtract two three-digit numbers by <u>counting back</u> in h, t and o</i> <i>eg. 763 - 121 as 763 - 100 - 20 - 1</i> <i>Subtract near multiples of 10 and 100</i> <i>eg. 648 - 199 as (648 - 200) + 1</i></p> <p>Counting up <i>Find the difference between two numbers by <u>counting up</u> from the smaller to larger eg. 121-87</i></p> <p>Using number facts <i>Number bonds to 100 eg. 100 - 35 = 65, 100 - 48 = 52 etc.</i></p>		<p>Vary the position of the answer and question.</p> <p>Expose children to missing number questions and vary the missing part of the calculation.</p> <p>678 = ? - 1 688 - 10 = ? 678 = ? - 100</p> 															
Using the bar to find missing digits. <i>It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.</i>		<table border="1" data-bbox="940 710 1254 837"> <tr><td>315</td><td></td></tr> <tr><td>185</td><td>?</td></tr> </table> <p>315 - 185 = ? 185 + ? = 315</p> <table border="1" data-bbox="940 909 1254 1029"> <tr><td>?</td><td></td></tr> <tr><td>185</td><td>315</td></tr> </table> <p>185 + 315 = ? ? - 185 = 315</p>	315		185	?	?		185	315	<table border="1" data-bbox="1568 718 2116 829"> <tr><td>435</td><td></td></tr> <tr><td>273</td><td>?</td></tr> </table> <table border="1" data-bbox="1859 718 2116 829"> <tr><td>435</td></tr> <tr><td>273</td><td>← ?</td></tr> </table> 	435		273	?	435	273	← ?
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	Concrete	Pictorial	Abstract
Subtracting tens and ones Subtract with up to 4 digits. Introduce decimal subtraction through context of money	<p style="text-align: center;">$234 - 179$</p> <p style="text-align: center;">Model process of exchange using Numicon, base ten and then move to PV counters.</p>	Children to draw place value counters and show their exchange—see Y3	<p style="text-align: center;">Use the phrase 'take and make' for exchange</p>
Mental Strategies	<p>Using place value <i>Count back in thousands</i> eg. $4378 - 3000$ as $4378, 3378, 2378, 1378$ <i>Take away multiples of 10, 100, 1000 and £1</i> eg. $8392 - 50$ or $6723 - 3000$ <i>Partitioning</i> eg. $£5.87 - £3.04$ as $£5 - £3$ and $7p - 4p$ or $7493 - 2020$ as $7000 - 2000$ and $90 - 20$</p> <p>Counting back <i>Count back</i> eg. $6482 - 1301$ as $6482 - 1000$ then $- 300$ then $- 1$ <i>Subtract near multiples of 10, 100 and 1000</i> eg. $3522 - 1999$ as $(3522 - 2000) + 1$</p> <p>Counting up <i>Find a larger difference between two numbers by counting up from the smaller number to the larger number</i> eg. $1506 - 387$</p> <p>Using number facts <i>Number bonds to 100 and to the next multiple of 100</i> eg. $100 - 76 = 24$ <i>Adjustment when adding 9 and 11</i> eg. $27 - 9$ as $(27 - 10) + 1$ or $36 - 11$ as $(36 - 10) - 1$</p>		

	Concrete	Pictorial	Abstract
<p>Using the bar to find missing digits.</p> <p><i>It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.</i></p>	<p>4,357</p>	<p>There are 3,160 books in a shop. 1,226 are in English and the rest are in French. How many French books are there?</p>	

Year 3 Multiplication

lots of, groups of, repeat, times, multiply, multiplied by, multiple of, double, part-part whole, short multiplication, inverse, product, factor.

	Concrete	Pictorial	Abstract
<p>Children should be able to recall the 2, 5, 10, 4 and 8 times tables.</p>			
<p>Mental calculations</p>	<hr/> <p>Count in steps – sequences <i>Count in 2s, 3s, 4s, 5s, 8s and 10s</i> eg. colour the multiples on a 100 square or jumps on a landmarked number line</p> <p>Doubling and halving <i>Find doubles to double 50 using partitioning</i> <i>Use doubling as a strategy in multiplying by 2 eg. 18 x 2 is double 18.</i></p> <p>Grouping <i>Recognise that multiplying is commutative eg. 8x4 = 4x8</i> <i>Multiply multiples of 10 by a single-digit eg. 30x8 = 240 (3x8=24)</i> <i>Multiply friendly two-digit numbers by single digit numbers eg. 13 x 4 = 52</i></p> <p>Using number facts <i>Know 2x, 3x, 4x, 5x, 8x and 10x</i></p> <hr/>		

Concrete	Pictorial	Abstract
<p>Count in steps – sequences <i>Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s</i></p> <p>Doubling and halving <i>Find doubles to double 100 and beyond using partitioning, using derived facts</i> <i>Begin to double amounts of money eg. £3.50 doubled is £7</i> <i>Use doubling as a strategy in multiplying by 2, 4 and 8</i> <i>eg. 34×4 is double 34 and double again.</i></p> <p>Grouping <i>Use partitioning to multiply two-digit numbers by single-digit numbers</i> <i>Multiply multiples of 100 by single-digit numbers using table facts eg. $400 \times 8 = 3200$ ($4 \times 8 = 32$)</i> <i>Multiply using near multiples by rounding eg. 24×19 as $(24 \times 20) = 24$</i></p> <p>Using number facts <i>Know times tables up to 12×12</i></p>	 	

Year 3 Division

divided by, divided into, sharing, into groups, halve, share, one each... two each... three each etc., left over, how many groups? Part, whole, equal groups, remainder

Division in year 3 is taught in relation to the times tables and begins to be explored in this way.

Year 4/5 Addition

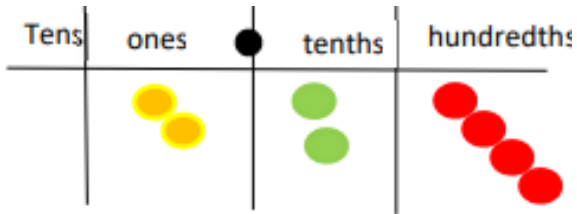
Addends, add, addition, plus, make, more, sum, total, increase, partition, column boundary, exchange, decimal, part, whole (Taught within recap sessions).

Adding numbers with more than 4 digits including decimals

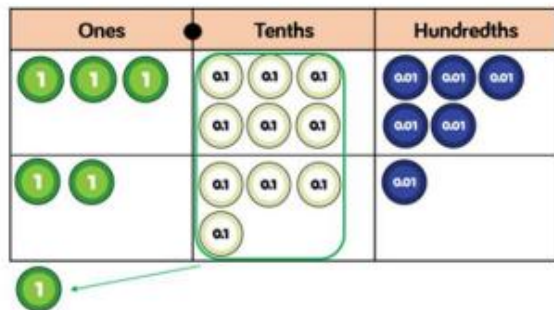
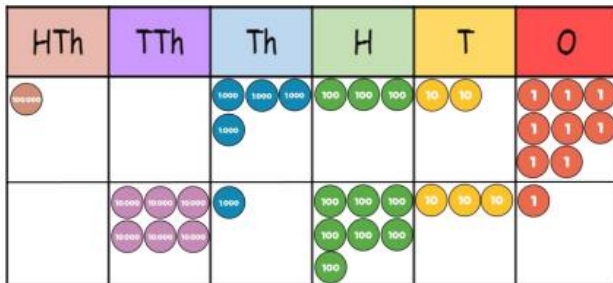
Using place value charts are key to this as well as place value counters to help with the decimals.

Concrete

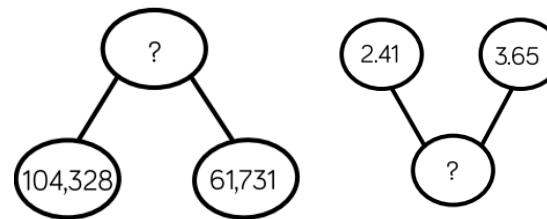
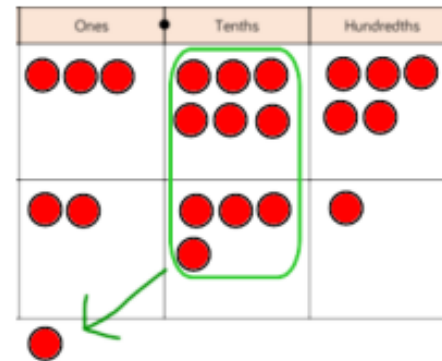
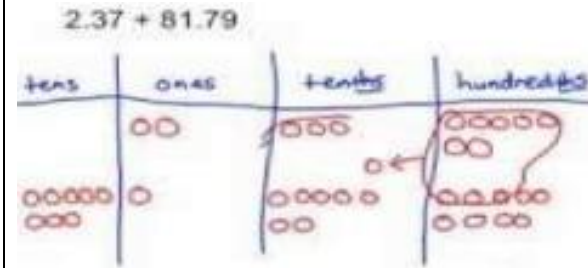
See Year 4 for other concrete methods.



Introduce decimal place value counters and model exchange for addition.



Pictorial



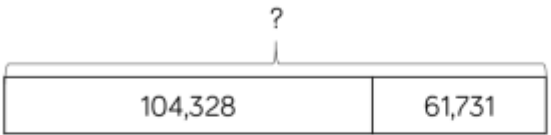
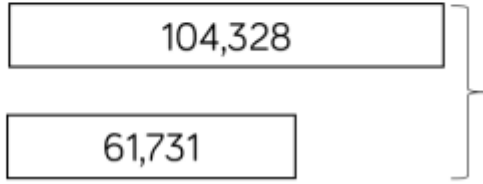
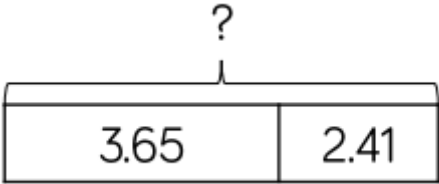
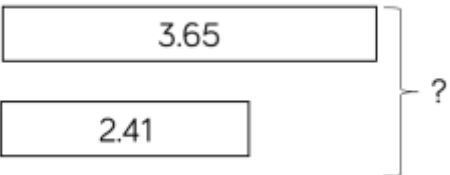
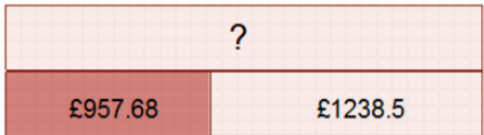

Abstract

$$\begin{array}{r} \text{£} 23.59 \\ + \text{£} 7.55 \\ \hline \text{£} 31.14 \end{array}$$

$$\begin{array}{r} 23481 \\ + 1362 \\ \hline 24843 \end{array}$$

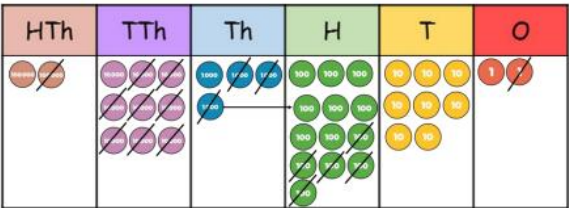
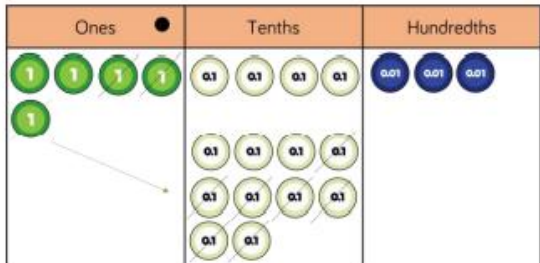
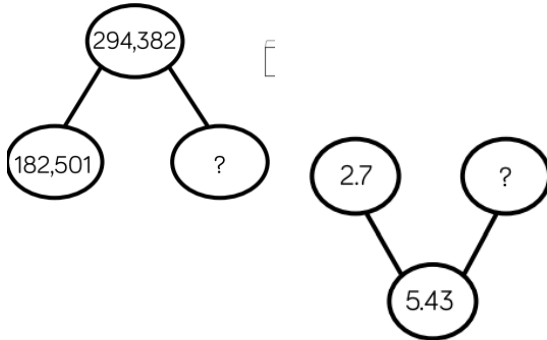
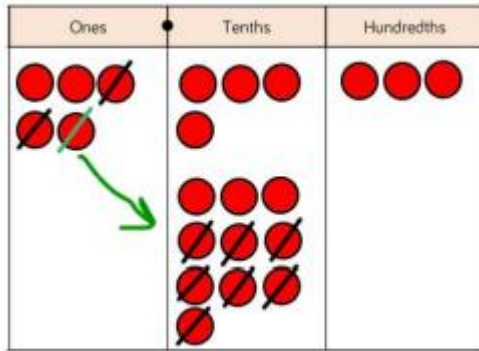

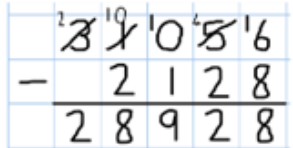
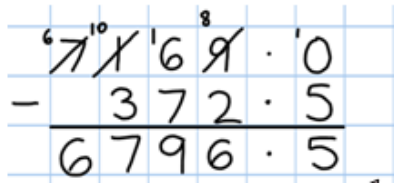
$$\begin{array}{r} 19.01 \\ 3.65 \\ + 0.7 \\ \hline 23.36 \end{array}$$

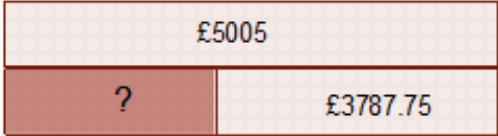
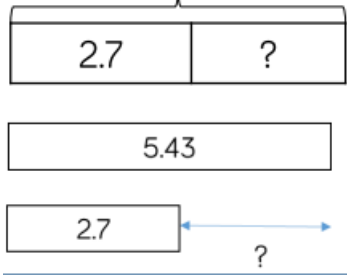
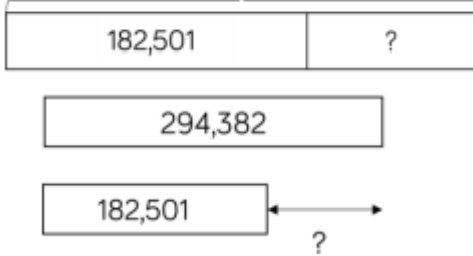


$$\begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ 1 \end{array}$$

	Concrete	Pictorial	Abstract
<p>Using the bar to find missing digits.</p> <p><i>It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.</i></p>	<p>This is not a form of getting the correct answer but helping to guide children to the correct operation.</p>  	<p>MacDonalds sold £9957.68 worth of hamburgers and £1238.5 worth of chicken nuggets. How much money did they take altogether?</p>  	
<p>Mental Strategies</p>	<p>Using place value <i>Count in steps of 10, 100, 1000, 0.1s, 0.01s from any given number.</i> <i>Partitioning eg. $7348 + 2187$ as $7348 + 2000 + 100 + 80 + 7$ or $2.4 + 5.8$ as $2 + 5, 0.4 + 0.8$ and combine the totals together.</i></p> <p>Counting on <i>Count on from the greatest number eg. $6834 + 3005$ as $9834 + 5$</i> <i>Add near multiples eg. $82,472 + 30,004$ as $(82,472 + 30,000) + 4$</i> <i>Add two decimal numbers by adding the o then ths then hths</i> <i>eg. $5.72 + 3.05$ as $5.72 + 3 + 0.5$</i></p> <p>Using number facts <i>Know number bonds to 1 and to the next whole number eg. $0.4 + 0.6$ or $5.7 + 0.3$</i> <i>Add to the next 10 from a decimal number eg. $7.8 + 2.2 = 10$</i></p> 		

Year 4/5 Subtraction

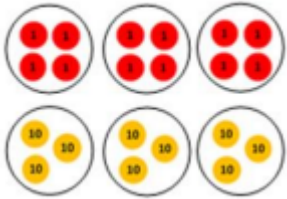



Minuend, subtrahend, subtract, subtraction, take away, minus, difference, decrease, exchange, decimal, part, whole (Taught within recap sessions).

	Concrete	Pictorial	Abstract
<p>Subtract with at least four digit numbers including two decimal places.</p> <p>Subtract with decimal values, including mixtures of integers and decimals, aligning the decimal point.</p> <p><i>Include money, measures and decimals ensuring that children do this practically before the abstract.</i></p>	<p>See Year 4</p> <div style="text-align: right; margin-right: 20px;">PV</div>  <p>counters</p> <div style="text-align: right; margin-right: 20px;">Plain</div>  <p>counters on the PV chart</p>	<p>Children to draw pv counters and show their exchange—see Y3</p>  	   <p style="text-align: center;">Use zeros for placeholders.</p> <div style="text-align: right;"> $\begin{array}{r} 41 \\ 5.43 \\ - 2.7 \\ \hline 2.73 \end{array}$ </div>

	Concrete	Pictorial	Abstract
<p>Using the bar to find missing digits.</p> <p><i>It is important for children to use the bar in this way to encourage the use of it to aid with problem solving.</i></p>	<p>Cuisenaire rods</p> <p>A whole to Lapland costs £5005 for a family of four, the Smith's have only saved £3787.75, how much money do they still need to find?</p> 	<p>5.43</p> 	<p>294,382</p> 
<p>Mental Strategies</p>	<p>Taking away <i>Use place value to subtract decimals eg. $4.58 - 0.08$ or $6.26 - 0.2$ etc.</i> <i>Take away multiples of power of 10 eg. $15,672 - 300$ or $4.82 - 2$</i> <i>Partition or count back eg. $3964 - 1051$ or $5.72 - 2.01$</i> <i>Subtract near multiples eg. $86,456 - 9999$ or $3.58 - 1.99$</i></p> <p>Counting up <i>Find a difference between two numbers by counting up from the smaller to the greater number eg. $2009 - 869$</i></p>  <p><i>Find change using shopkeepers' addition eg. buy toy for £6.89 using £10</i></p>  <p>Using number facts <i>Derived facts from number bonds to 10 and 100 eg. $2 - 0.45$ using $45 + 55 = 100$</i> <i>Number bonds to £1, £10 and £100 eg. $£4.00 - £3.86 = 14p$</i></p>		

Year 4/5 Multiplication

Multiplier, multiplicand, product, lots of, groups, times, multiply, multiplied by, multiple of, short multiplication, long multiplication, part, whole, square numbers, cube numbers, prime numbers, factors and prime factors.

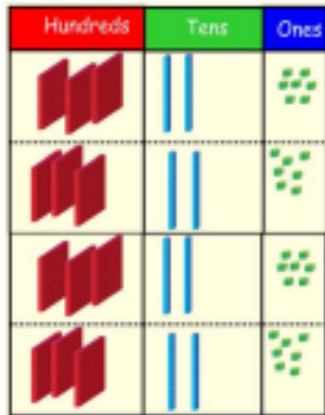
	Concrete	Pictorial	Abstract																																																																																																																					
<p>Children to know all times tables to 12 x 12.</p> <p>Expanded column method to be used with children multiplying both two and three digits by a one digit number.</p>	<p>Build numbers using PV counters</p> <p>34×3</p>  <p>473×2</p> <table border="1" style="margin-left: auto; margin-right: auto; text-align: center;"> <tr> <td style="background-color: #ccccff;">100</td><td style="background-color: #ccccff;">100</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffcccc;">1</td><td style="background-color: #ffcccc;">1</td> </tr> <tr> <td style="background-color: #ccccff;">100</td><td style="background-color: #ccccff;">100</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td></td><td style="background-color: #ffcccc;">1</td><td></td> </tr> <tr> <td style="background-color: #ccccff;">100</td><td style="background-color: #ccccff;">100</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffcccc;">1</td><td style="background-color: #ffcccc;">1</td> </tr> <tr> <td style="background-color: #ccccff;">100</td><td style="background-color: #ccccff;">100</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td style="background-color: #ffffcc;">10</td><td></td><td style="background-color: #ffcccc;">1</td><td></td> </tr> </table> 	100	100	10	10	10	10	1	1	100	100	10	10	10		1		100	100	10	10	10	10	1	1	100	100	10	10	10		1		<p>Children can draw place value counters in books</p> <p>$34 \times 3 =$</p> 	<table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">h</td><td style="text-align: center;">t</td><td style="text-align: center;">o</td><td></td> </tr> <tr> <td></td><td style="text-align: center;">3</td><td style="text-align: center;">4</td><td></td> </tr> <tr> <td style="text-align: center;">x</td><td></td><td style="text-align: center;">3</td><td></td> </tr> <tr> <td colspan="3" style="border-top: 1px solid black;"></td><td></td> </tr> <tr> <td></td><td style="text-align: center;">1</td><td style="text-align: center;">2</td><td style="text-align: right;">(4 x 3)</td> </tr> <tr> <td colspan="3" style="border-top: 1px solid black;"></td><td></td> </tr> <tr> <td></td><td style="text-align: center;">9</td><td style="text-align: center;">0</td><td style="text-align: right;">(30 x 3)</td> </tr> <tr> <td colspan="3" style="border-top: 1px solid black;"></td><td></td> </tr> <tr> <td style="text-align: center;">1</td><td style="text-align: center;">0</td><td style="text-align: center;">2</td><td style="text-align: right;">3 1 4</td> </tr> <tr> <td colspan="3" style="border-top: 1px solid black;"></td><td style="text-align: right;">x 3</td> </tr> <tr> <td></td><td></td><td></td><td style="text-align: right;">12 (3 x 4)</td> </tr> <tr> <td></td><td></td><td></td><td style="text-align: right;">30 (3 x 10)</td> </tr> <tr> <td></td><td></td><td></td><td style="text-align: right;">+ 900 (3 x 300)</td> </tr> <tr> <td colspan="3" style="border-top: 1px solid black;"></td><td style="text-align: right;"><u>942</u></td> </tr> </table> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td><td style="text-align: center;">327</td> </tr> <tr> <td></td><td style="text-align: center;">x 4</td> </tr> <tr> <td colspan="2" style="border-top: 1px solid black;"></td> </tr> <tr> <td></td><td style="text-align: center;">28</td> </tr> <tr> <td></td><td style="text-align: center;">80</td> </tr> <tr> <td></td><td style="text-align: center;">1200</td> </tr> <tr> <td></td><td style="text-align: center;">1308</td> </tr> </table>  <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">3</td><td style="text-align: center;">2</td><td style="text-align: center;">7</td> </tr> <tr> <td style="text-align: center;">x</td><td></td><td style="text-align: center;">4</td> </tr> <tr> <td colspan="3" style="border-top: 1px solid black;"></td> </tr> <tr> <td style="text-align: center;">1</td><td style="text-align: center;">3</td><td style="text-align: center;">0</td> </tr> <tr> <td style="text-align: center;">8</td><td></td><td></td> </tr> </table>	h	t	o			3	4		x		3							1	2	(4 x 3)						9	0	(30 x 3)					1	0	2	3 1 4				x 3				12 (3 x 4)				30 (3 x 10)				+ 900 (3 x 300)				<u>942</u>		327		x 4				28		80		1200		1308	3	2	7	x		4				1	3	0	8		
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Concrete

Multiplying up to four digit numbers by two digits using long multiplication.

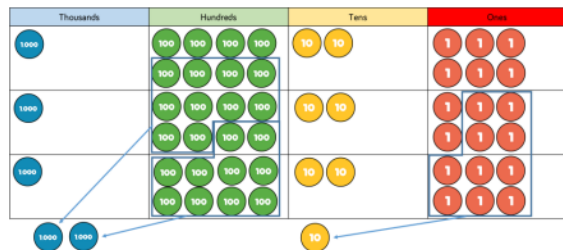
Children need to be taught to approximate first, e.g. for 72×38 , they will use **rounding**: 72×38 is approximately $70 \times 40 = 2800$, and use the approximation to check the reasonableness of their answer.

$$327 \times 4 =$$



Children can continue to be supported by place value counters at the stage of multiplication.

If children are

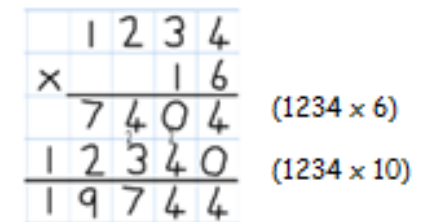
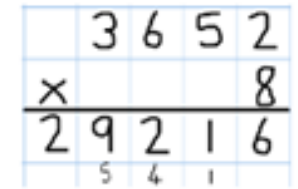


struggling with times tables knowledge, they can use multiplication squares so they can concentrate on the method.

Pictorial

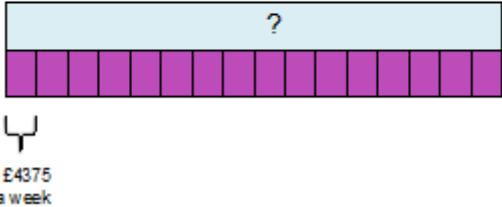


Pictorial representations of manipulatives.

Abstract



Long multiplication- Model the place holder in a separate colour so children remember it and know you are multiplying by a multiple of 10.

	Th	H	T	O
		2	3	4
x			3	2
		4	6	8
17	10	2	0	
7	4	8	8	

	Concrete	Pictorial	Abstract
Using the bar model to support multiplication.	<p>The cost to run a sports centre is £4375 a week, how much would it cost to run for 16 weeks?</p> 		
Mental Strategies	<hr/> <p>Doubling and halving <i>Use double and halving strategies when multiplying by 2, 4, 8, 5 and 2½</i> <i>Double amounts of money using partitioning eg. £6.73 doubled is double £6 plus double 73p</i></p>  <p>Grouping <i>Multiply decimals by 10, 100 and 1000 eg. 3.4 x 100 = 340</i> <i>Use partitioning to multiply friendly two-digit and three-digit numbers by single digits eg. 402 x 6 as (400x6) + (2 x 6)</i> <i>Use partitioning to multiply decimal numbers by single digit numbers eg. 4.5 x 3 as (4x3) + (4x0.5)</i> <i>Multiply using near multiples by rounding eg. 32 x 29 as (32 x 30) - 32</i></p>  <p>Using number facts <i>Use times tables facts up to 12x12 to multiply multiples of the multiplier eg. 6 x 4 = 24 so 60 x 4 = 240 and 600 x 4 = 2400</i> <i>Know square numbers and cube numbers</i></p>		

Year 4/5 Division

Dividend, divisor, quotient, sharing, share equally, into groups, divided by, divided into, left over, remainder, how many groups, factor, prime factor, divisible by, divisibility, inverse, part, whole, cube numbers, square numbers

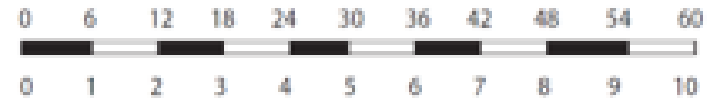
Concrete

Pictorial

Abstract

Count in steps – sequences

Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s



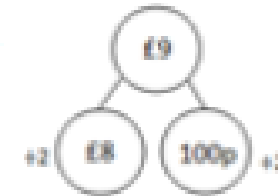
Doubling and halving

Find halves of even numbers to 200 and beyond using partitioning, using derived facts

Begin to halve amounts of money eg. £9 halved is £4.50

Use halving as a strategy in dividing by 2, 4 and 8

eg. $164 \div 4$ is half of 164 and halved again.



Grouping

Use multiples of 10 times the divisor to divide by numbers <10 eg. $45 \div 3$ as $30 \div 3$ and $15 \div 3$

Divide multiples of 100 by single digits numbers using division facts eg. $3200 \div 8 = 400$

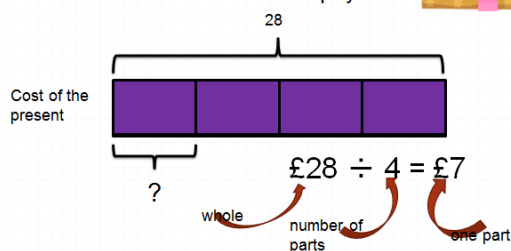
Using number facts

Know times tables up to 12×12 and all related division facts

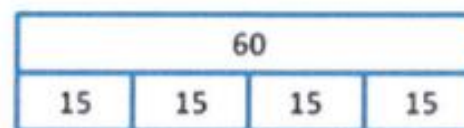
Use division facts to find unit and non-unit fractions of amounts

Using the bar to aid the solving

Four children bought a present for £28. They shared the costs equally. How much did each child pay?



$$60 \div 4 = 15$$



'60 in four equal parts'

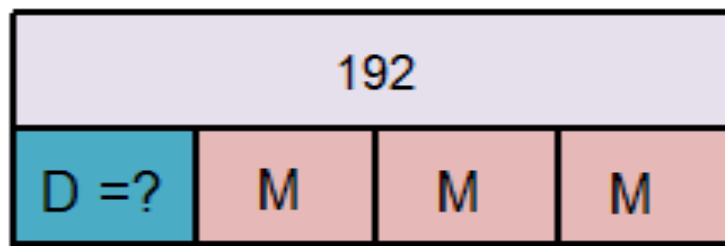
$$28 \div 7 = 4$$



'How many 7s in 28?'

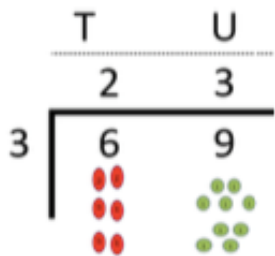
of division problems.

Desmond and Melissa collect cards. They have 192 cards in all. Melissa has three times as many cards as Desmond. How many cards does Desmond have?



Dividing using short division.

Once children are secure with division as grouping and demonstrate this using number lines, arrays etc., **short division** for larger 2-digit numbers should be introduced, initially with carefully selected examples requiring no calculating of remainders at all. Start by introducing the layout of short division by comparing it to an array.

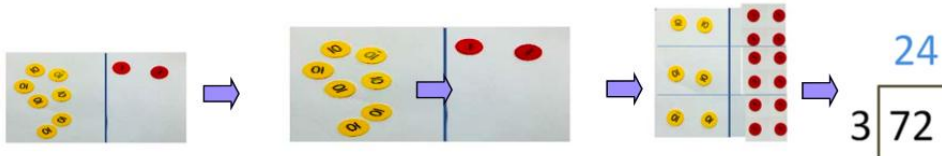


Remind children of correct place value, that 69 is equal to 60 and 9, but in short division, pose:

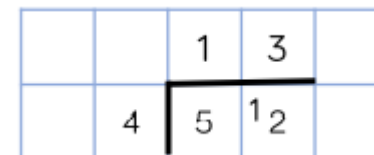
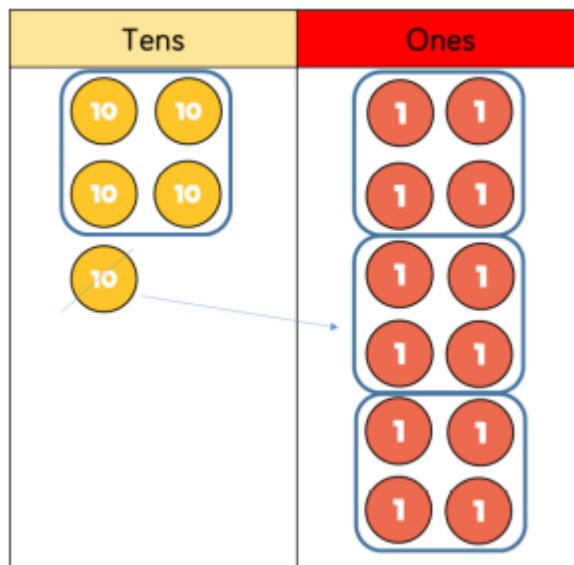
· How many 3's in 6? = 2, and record it above the 6 **tens**.

How many 3's in 9? = 3, and record it above the 9 **ones**.

Once children demonstrate a full understanding of remainders, and also the short division method taught, they can be taught how to use the method when remainders occur within the calculation (e.g. $72 \div 3$), and be taught to 'carry' the remainder onto the next digit.

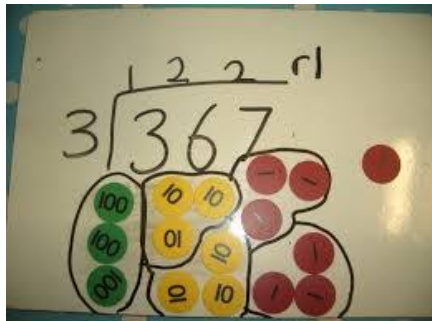


$52 \div 4 = 13$



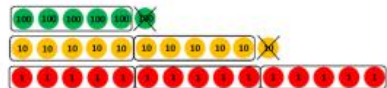
Diving with up to four digit numbers by one digit including numbers where remainder s are left.

Short division with remainders: Now that pupils are introduced to examples that give rise to remainder answers, division needs to have a real life problem solving context, where **pupils consider the meaning of the remainder and how to express it**, ie. as a fraction, a decimal, or as a rounded number or value , depending upon the context of the problem.



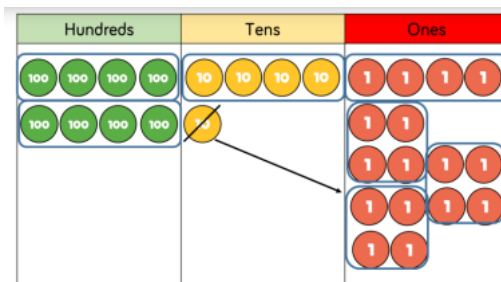
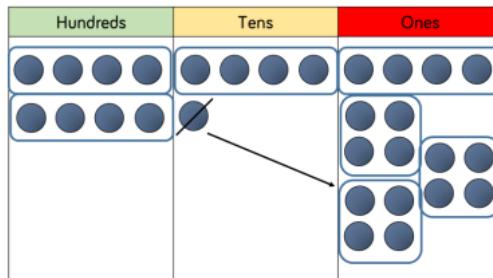
With regrouping

$$\begin{array}{r} 1 \ 2 \ 3 \\ 5 \overline{) 6 \ 1 \ 5} \end{array}$$



(children could use concrete counters or draw working out as a pictorial representation)

Children can replicate place value counters as drawings to support bus stop division and how many groups can be made each time.



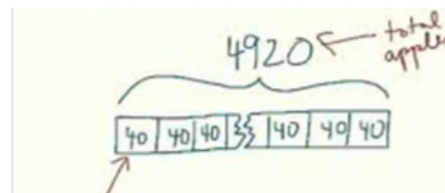
$$\begin{array}{r} 0 \ 5 \ 6 \ 7 \\ 9 \overline{) 5 \ 1 \ 0 \ 3} \end{array}$$

$$\begin{array}{r} 0 \ 6 \ 6 \ 3 \ r \ 5 \\ 8 \overline{) 5 \ 3 \ 0 \ 9} \end{array}$$

Using the bar to support division problems.

Bar Model to support understanding of problem solving:

Frank has 4920 apples. He needs to put them into baskets of 40. How many baskets does he need?



Mental Strategies

Doubling and halving

Halve amounts of money using partitioning eg. half of £14.84 is half of £1 and half of 84p



Use doubling and halving as a strategy in dividing by 2, 4, 8, 5 and 20 eg. $115 \div 5$ as double $115 \div 10$

Grouping

Divide numbers by 10, 100, 1000 to obtain decimal answers with up to three places eg. $340 \div 100 = 3.4$

Use 10^{th} , 20^{th} , 30^{th} multiples of the divisor to divide friendly two-digit and three-digit numbers

eg. $186 \div 6$ as $180 \div 6$ plus $6 \div 6$

Find unit and non-unit fractions of large amounts eg. $\frac{3}{5}$ of 265 is $3 \times (265 \div 5)$

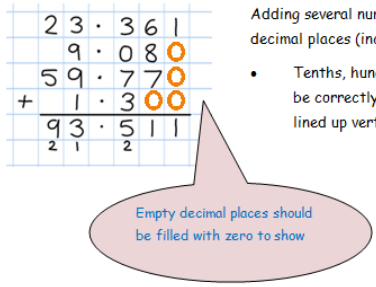


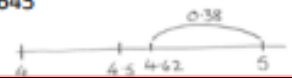
Using number facts

Use division facts up to 12×12 to divide numbers by single-digit numbers eg. $3600 \div 9$ as $36 \div 9$

Know square numbers and cube numbers

Year 6 Addition

Addends, add, addition, plus, make, more, sum, total, increase, partition, column boundary, exchange, decimal, part, whole,

	Concrete	Pictorial	Abstract						
<p>Compact column addition to add numbers with up to 6 digits.</p> <p>Adding several numbers with up to three decimal places. Money and measures</p>	<p><u>See Years 3/4 and 5</u></p>	<p><u>See Years 3/4 and 5</u></p>  <p>Adding several numbers with different numbers of decimal places (including money and measures):</p> <ul style="list-style-type: none"> Tenths, hundredths and thousandths should be correctly aligned, with the decimal point lined up vertically including in the answer row. 							
<p>Adding using the bar.</p>	<p>Jack went on holiday. His flight cost £70.50, the hotel £1295 and spending money £427.89. How much did Jack spend on his holiday?</p>	<table border="1" data-bbox="806 853 1254 965"> <tr> <td colspan="3" style="text-align: center;">?</td> </tr> <tr> <td style="text-align: center;">£70.50</td> <td style="text-align: center;">£427.89</td> <td style="text-align: center;">£1295</td> </tr> </table>	?			£70.50	£427.89	£1295	
?									
£70.50	£427.89	£1295							
<p>Mental Strategies</p>	<p>Using place value <i>Count in 0.1s, 0.01s, and 0.001s eg. knowing what 0.001 more than 6.725 is</i> <i>Partitioning eg. 9.54 + 3.25 as 9 + 3 and 0.5 + 0.2 and 0.04 + 0.05 to get 12.79</i></p>  <p>Counting on <i>Add two decimal numbers by adding the o then ths then hths or tths</i> eg. 6.31 + 3.46 as 6.31 + 3 + 0.4 + 0.06 <i>Add near multiples to 1 and 10 eg. 6.75 + 9.95 as (6.75 + 10) - 0.05 or 6.35 + 0.99 as (6.35 + 1) - 0.01</i></p> <p>Using number facts <i>Number bonds to 1 and to the next multiple of 1 eg. 0.63 + 0.37 or 2.35 + 0.645</i> <i>Add to the next ten eg. 4.62 + 0.38</i></p> 								

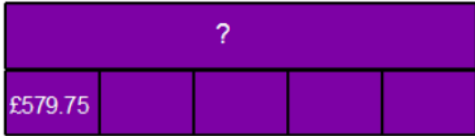
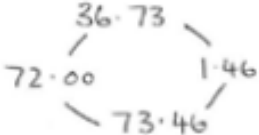
Year 6 Subtraction

Minuend, subtrahend, subtract, subtraction, take away, minus, difference, decrease, exchange, decimal, part, whole

	Concrete	Pictorial	Abstract						
Subtracting with increasingly large and more complex numbers and decimal values (up to 3dp)	Very important to use in a range of contexts-measures and money. <u>See Years 3/4 and 5</u>	<u>See Years 3/4 and 5</u>							
Using the bar for subtraction.	Chloe wants to buy a new car for £6450. She has £4885.87 in her savings account. Her Dad gives her £150 for her birthday. How much more money does she need to save? <div style="text-align: center; margin-top: 10px;"> <table border="1" style="margin: auto; border-collapse: collapse;"> <tr> <td colspan="3" style="text-align: center; padding: 5px;">£6450</td> </tr> <tr> <td style="padding: 5px;">£4885.87</td> <td style="padding: 5px;">£150</td> <td style="padding: 5px;">?</td> </tr> </table> </div>			£6450			£4885.87	£150	?
£6450									
£4885.87	£150	?							
Mental Strategies	<p>Taking away Use place value to subtract decimal numbers eg. $7.78 - 0.08$ or $16.26 - 0.2$ etc Take away multiples of power of 10 eg. $123,956 - 400$, $686,109 - 40,000$ or $7.82 - 0.5$ Partition or count back eg. $3964-1051$ or $5.72 - 2.01$ Subtract near multiples eg. $360,078 - 99,998$ or $12.83 - 0.99$</p> <p>Counting up Count up to subtract numbers from multiples of 10, 100, 1000, 10,000 Find a difference between two decimal numbers by counting up from the smaller the greater number eg. $1.2 - 0.87$</p> <div style="text-align: center; margin-top: 10px;"> </div> <p>Using number facts Derive facts from number bonds to 10 and 100 eg. $5 - 0.65$ Number bonds to £1, £10 and £100 eg. $£7.00 - £4.37$</p> <div style="text-align: center; margin-top: 10px;"> </div>								

Year 6 Multiplication

Multiplier, multiplicand, product, lots of, groups, times, multiply, multiplied by, multiple of, short multiplication, long multiplication, part, whole, square numbers, cube numbers, prime numbers, factors and prime factors.

Concrete	Pictorial	Abstract
<p>Short and long multiplication of whole integers and with up to two decimal places.</p>	<p><u>See Years 3/4 and 5</u></p>	<p><u>See Years 3/4 and 5</u></p>
<p>Using the bar to help with multiplication.</p>	<p>If 5 friends went on holiday and each paid £579.75 what was the total cost of the holiday?</p> <p>Cost of the holiday</p> 	
<p>Mental Strategies</p>	<p>Doubling and halving <i>Use doubling and halving as strategies in mental multiplication. Double decimal numbers with up to 2 places using partitioning eg. 36.73 doubled is double 36 (72) plus double 0.73 (1.46)</i></p>  <p>Grouping <i>Use partitioning as appropriate eg. 3060 x 4 as (3000x4) + (60 x 4) or 8.4 x 8 as (8 x 8) + (0.4 x 8)</i> <i>Use factors in mental multiplication eg. 421 x 6 as 421 x3 and doubled or 3.42 x 5 is half of 3.42 x 10</i> <i>Multiply decimal numbers using near multiples by rounding eg. 4.3 x 19 as (4.3 x 20) – 4.3</i></p> <p>Using number facts <i>Use times tables facts up to 12x12 in mental multiplication of large numbers or numbers with up to two-decimal places eg. 6 x 4 = 24 so 0.06 x 4 = 0.24</i></p>	

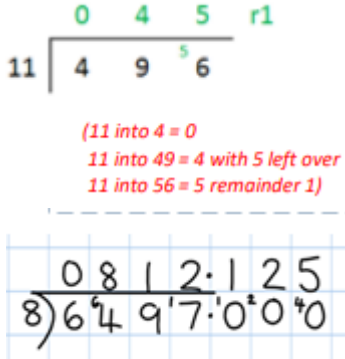
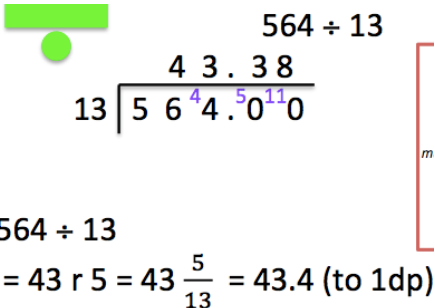
Abstract

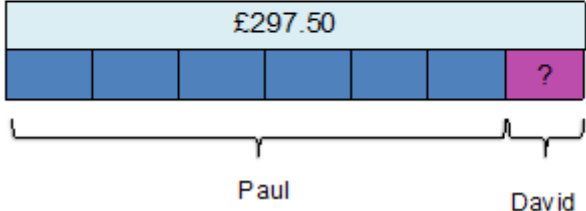

Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer.

$$\begin{array}{r}
 3.19 \\
 \times 8 \\
 \hline
 25.52
 \end{array}$$

Year 6 Division

Dividend, divisor, quotient, sharing, share equally, into groups, divided by, divided into, left over, remainder, how many groups, factor, prime factor, divisible by, divisibility, inverse, part, whole, cube numbers, square numbers

Concrete		Pictorial	Abstract
<p>Divide at least 4 digits by single-digit (including decimal numbers and quantities)</p>	<p>Short division with remainders: Pupils should continue to use this method, but with numbers to at least 4 digits, and understand how to express remainders as fractions, decimals, whole number remainders, or rounded numbers. Real life problem solving contexts need to be the starting point, where pupils have to consider the most appropriate way to express the remainder.</p>		 <p style="text-align: center;"> $11 \overline{) 4956} \text{ r}1$ <i>(11 into 4 = 0 11 into 49 = 4 with 5 left over 11 into 56 = 5 remainder 1)</i> </p>
<p>Long division this is for when dividing by two digit numbers. Use the short bus stop method with known facts listed alongside.</p> <p>Express remainders as fractions or decimals</p>		 <p style="text-align: center;"> $564 \div 13$ $13 \overline{) 564.00}$ $564 \div 13 = 43 \text{ r} 5 = 43 \frac{5}{13} = 43.4 \text{ (to 1dp)}$ </p>	<p>Known facts by partitioning</p> <p>10+3=13 20+6=26 30+9=39 40+12=52 etc</p>

	Concrete	Pictorial	Abstract
Using the bar to help divide.	<p data-bbox="421 220 936 306">Paul and David hire a car together at a cost of £297.50. Paul pays 6 times more than David. How much does David pay?</p> 		
Mental Strategies	<p data-bbox="331 593 1214 746">Doubling and halving <i>Use doubling and halving as strategies in mental division.</i> <i>Halve decimal numbers with up to two-places using partitioning</i> eg. half of 38.86 is half of 38 plus half of 0.86.</p>  <p data-bbox="331 778 1648 932">Grouping <i>Use 10th, 20th, 30th ... 100th, 200th etc. multiples of the divisor to divide larger numbers eg. 378 ÷ 9 as 360 ÷ 9 and 18 ÷ 9.</i> <i>Use tests for divisibility eg. 135 divides by 3 as 1+3+5 = 9 and 9 is in the 3x tables.</i></p> <p data-bbox="331 970 1603 1078">Using number facts <i>Use division facts up to 12x12 to divide decimal numbers by single-digit numbers eg. 1.17 ÷ 3</i> 1/100 of 117 ÷ 3 (0.39)</p>		